1 Introduction

Lawmakers throughout the U.S. have mandated that a significant percentage of electricity supply should be derived from renewable resources. Each state has set its own goal, with California being the most aggressive, requiring 50% renewables by 2026, 60% by 2030, and 100% by 2045 (see [22]). State and local authorities (e.g., independent system operators (ISOs)) have commissioned studies to assess operational considerations such as system reliability, market design, incorporation of storage technologies, and other avenues. A recent simulation study [18], commissioned by California ISO (CAISO), suggests that for renewable-integration levels beyond 33%, one can expect a fair amount of over-generation and renewable curtailment during daytime, and perhaps, load-shedding around sundown. These issues are exacerbated at higher levels of renewable penetration, and maintaining system reliability becomes a challenge.

A popular illustration of the above issues are captured by the so-called “duck-chart” of CAISO (see Fig. 1). This figure depicts the daily net-load (total electric load minus generation from “must-run” units) across successive years with increasing levels of solar added to the generation mix. A surplus of solar energy during daytime leads to a dip in the net-load, followed by a significant upward ramp around sundown. In a grid with limited storage capabilities, excess supply during daytime poses significant challenges as utilities will be required to procure sufficient ramp-up capabilities to meet the electric load of evening hours. The absence of substantial ramping capabilities can push the loss-of-load probability to unacceptable levels, and may even cause load-shedding in certain areas, jeopardizing system reliability and performance.

On the other hand, over-generation during daytime could lead to negative prices in the market, resulting in, for instance, large shipments of energy to neighboring states (e.g., from California to Arizona), while paying these states to accept the surplus at home (see [21]).

![Duck Chart](image.png)

Figure 1: CAISO’s duck chart, predicting four emerging ramping patterns with increased renewable integration [4].

In order to meet the challenges discussed above and “tame the duck”, so to speak, a recent U.S. Department of Energy (DOE) report [3] has distilled a myriad of operational guidelines (for maintaining reliability) into four specific rules:

- Power generation and transmission capacity must be sufficient to meet peak demand for electricity;
• Power systems must have adequate flexibility to address variability and uncertainty in demand and generation resources;
• Power systems must be able to maintain steady frequency;
• Power systems must be able to maintain steady voltage at various points on the grid.

These rules are particularly focused on changes that are expected over the next several years due to the inclusion of new production resources, especially variable energy resources (VER). The first two rules can be seen as addressing operations planning, whereas the last two rules pertain to operations control. The latter are typically addressed via controlling devices such as inverters. To quote a recent study associated with a photovoltaic (PV) demonstration project, the authors observe that modern inverters “mitigate the impact of [PV] variability on the grid, and contribute to important system requirements more like traditional generators” [14, p. 5]. Another innovation which is credited to improving power system control is flexible AC transmission systems. These devices used to be relatively expensive several years ago, but are relatively inexpensive now, and should be looked upon as part of the modern grid.

In contrast to the operations control studies, the focus of this paper is on the first two rules which are crucial for operations planning. While there are some current proposals for completely decentralized electricity production and markets, it is commonly accepted that the presence of an ISO enhances the reliability of the power system. Accordingly, our study is devoted to this setting.

Given the above focus, our plan is to explore the reliability impact of two alternative mechanisms for operations planning, both of which require coordination via a central planning authority (e.g. ISO). The first of these is the currently popular approach, which we refer to as the deterministic hierarchical planning (DHP) framework. Most ISOs in the U.S. currently implement some form of DHP framework, which divide the daily planning activities into three principal planning layers: a) the day-ahead unit commitment plan based on a daily forecast of load, generation capacities, as well as a transmission plan, b) the short-term unit commitment, with a shorter planning window (typically three to four hours) during which some commitment decisions and transmission plans are updated, c) the hour-ahead economic dispatch, whereby, the production and transmission plans are finalized, and if necessary, reserve capacities are committed. There are some variations of this multi-layer hierarchy, such as updating the dispatching plan in 15-minute intervals to accommodate high levels of VER. All layers for this setup use some form of deterministic optimization, and as such, all forecasts used in the optimization models should be considered as “point forecasts”.

Before we proceed, we want to note the distinction between a “model” and an “algorithm”. The former is used to express a particular mathematical structure used to state a decision problem. On the other hand, an algorithm is used to specify the computational steps which are undertaken to solve the mathematical model. Thus, a linear programming (LP) model, for example, states that linearity is a principal guiding force for the model, and any algorithm which solves LP models can be used as a solution methodology. However, we caution that not all algorithms which solve a particular class of models are equally effective in solving equivalent models. This is particularly true for stochastic programming (SP) models for which certain types of structures (e.g., fixed and complete recourse models with linear structures) are much more amenable to specialized solution algorithms, than general purpose SP algorithms [23].

Because of the degree of variability in load as well as VER, an alternative to DHP is stochastic hierarchical planning (SHP) with the main difference being that at each layer of the hierarchy, we allow a constrained stochastic programming setup, so that the decisions are cognizant of various uncertainties (load, generation, failures etc.). These models are solved using stochastic programming (SP) algorithms, some of which have been studied rigorously over the past twenty-five years [10, 11] with more recent versions in [24, 25]. In this paper we coalesce our re-
search from SP, including discrete SP [2], with the work in power systems research for economic dispatch (ED) [8, 7] and unit commitment (UC) [1].

As with DHP, we will use the suite of SHP models for operations planning using an academic dataset. We will compare the performance of these alternative suites of models, and examine questions which pertain to metrics corresponding to the operations planning rules of the DOE report. More specifically, the comparisons between DHP and SHP will focus on the following questions at different levels of penetration of VER.

- Are there significant differences between results for unmet demand for DHP v SHP? Does one dominate the other?
- Are there significant differences between conventional over-generation and renewable curtailment for DHP v SHP?
- To what degree does each approach rely on reserve generation?
- What percentage of daily power generation was due to short-term unit commitment?

In addition to the above system reliability questions, we will also compare costs and greenhouse gas (GHG) emissions. Our conclusions regarding the viability of these approaches will be based on these comparisons.

While there are many studies of stochastic optimization within any one layer of the hierarchical system (see [6, 29] for exhaustive reviews), no other study pits the standard hierarchy of deterministic models against a hierarchy of stochastic models. It is such a comparison which provides a preview of potential advantages and disadvantages of these alternative hierarchies. Thus, this study examines whether a system-wide overhaul which introduces stochastic optimization and coordination among all layers of the hierarchy can mitigate difficulties associated with high penetration of renewable energy into the grid. Our experiments point to the potential of such a transition to a SHP framework.

The remainder of the paper is arranged as follows. In §2 we present a detailed description of the SHP framework including the optimization models and solution algorithms employed. In §3 we present the experimental results conducted using the NREL118 dataset on the DHP and SHP frameworks. Finally, we will conclude with a brief discussion in §4.

2 Stochastic Hierarchical Planning

Electric power systems are very large-scale networks interconnecting many sources of electric power (generators) to points of consumption (loads). The entire network is arranged at several voltage levels, converted from one to the other by step-up or step-down transformers. This network is operated with the overall goal of minimizing total cost while ensuring reliable power delivery. The implementation of this objective is complex when viewed as a single decision making problem. Therefore, system operators use a reformulation involving a hierarchy of optimization models defined over overlapping horizons with different time resolutions for decisions and constraints.

The particular rules, design, and operational elements differ markedly across different system operators. In addition to the ISOs which oversee the operations over larger geographic areas, balancing area authorities (BAA) for smaller regions also operate under notably different practices. For instance, Bonneville Power Administration, which primarily oversees hydroelectricity production, performs bulk-hourly generation-scheduling, and has sufficient range of reserves and ramping capabilities for handling imbalances [15]. However, in the case of ISOs as well as BAAs, the operations can be classified into two phases: day-ahead (DA) and real-time (RT) [5, 16, 17]. In line with the current practices, we also adopt a hierarchical decision process comprising of DA and RT phases.
Day-ahead Operations

This phase begins by estimating demand and renewable-supplies as well as collecting generation and demand bids. This information is used in simultaneous co-optimization of the next operating day using security constrained UC and security constrained ED models. In our setting, these optimization models are formulated over a 24-hours horizon with decisions and constraints defined at an hourly resolution. The UC model commits and schedules resources for regulation. The DA planning also involves committing resources for reliability assessment and emergency operations, however, we do not consider these in our setup. The UC optimization model involves continuous as well as binary decision variables, resulting in a mixed integer program (MIP).

The UC decisions are used to instantiate the DA security constrained ED model. The ED model is used to determine the generation, regulating and spinning reserve amounts for all committed resources, as well as the ex ante DA prices. While the ED model in the DA phase is often solved separately for each hour of the day, we formulate the ED model as a single optimization model defined over an entire day at an hourly resolution. In our models we do not allow for generator self-scheduling and do not consider system operations under contingency/emergency.

Real-time Operations

There is always some RT deviation of actual generation and load from what was scheduled during DA planning. One of the key functions of the ISO is to perform real-time balancing of loads and generation. RT balance is maintained through the combined use of spinning and ancillary services along with the units providing regulation reserves, which are managed by the automatic generation control (AGC). The non-AGC units are dispatched every few minutes (usually 5 to 15 minutes), while the regulation units are used only to respond instantaneously to system imbalances.

In our setting we will use an Hour-ahead ED (HA-ED) model for balancing the supply and demand at least cost while recognizing the operating conditions of the system a few minutes ahead of the actual dispatch. The model will determine the generation quantities and reserve levels for non-AGC units. These models are defined at a resolution of 15 minutes and a horizon of 75 minutes. Furthermore, HA-ED model is solved every 15 minutes in a rolling horizon manner. This allows us to revise the generation amounts of committed units closer to the time of dispatch when updated forecasts are available.

Short-term Operations

Some of the advanced ISOs use additional instruments that commit fast-start resources in order to ensure that schedules meet all the reliability requirements. The associated models are solved independently against DA transactions and generation bids. At certain ISOs, these operations are considered to be part of the RT markets and are referred to as the RT-UC (e.g., NYISO). Following its usage at CAISO, we will refer to these operations as Short-Term UC (ST-UC). These models are formulated at finer resolution (15 minutes) that allows adaptive (de)commitment decisions, and are solved over a horizon of few hours (e.g., 4.5 hours at CAISO and 2.5 hours in NYISO). In our setting we define these models at a resolution of 15 minutes and a horizon of 4 hours.

In summary, the framework considered in this work comprises of three phases – day-ahead, short-term and real-time. These phases are arranged in a hierarchical manner with progressively (from DA to RT) shorter horizon, higher resolution, and using updated forecasts of demand and renewable generation. The interactions and timeline of our modeling framework are illustrated in Fig. 2. Notice that our framework does not involve an energy market, or ancillary services such as ramping reserves. We assume that the latter can serve any unmet demand that might
be revealed during our planning process, albeit at a higher cost. Finally, since the framework is focused on planning phases, we do not consider real-time AGC.

Even with this temporal decomposition, both generation scheduling and dispatch problems are truly stochastic optimization problems, and as such are computationally very challenging. Therefore, the power systems operators employ deterministic optimization methods that approximate these stochastic optimization models with static deterministic optimization models. Some ISOs (e.g., New England ISO) have recognized the shortcomings of deterministic planning within the context of renewable integration, and recommend certain deterministic policies (e.g., “do-not-exceed” limits on wind and hydro power [28]). In the absence of significant storage capacity in the system, such vast swings may result in over-generation, which, in turn, require bi-lateral agreements and exchanges between neighboring ISOs to ensure supply matches demand. Nevertheless, the current approaches to power systems operations remain beholden to deterministic models and policies. Our goal is to explore whether there are benefits to using stochastic optimization models within power systems planning, especially, in the context of high penetration levels of VER.

Accordingly, we will consider deterministic planning models as our benchmark. Then, we will investigate the potential of using stochastic optimization models, by replacing the deterministic approaches with their stochastic counterparts. We will next discuss the optimization models used in our framework.

2.1 Optimization Models

Both the UC and ED problems are fundamental to power systems planning and operations. These problems are posed as deterministic optimization models, often with linearized objective functions and constraints. Due to the presence of commitment decisions, which are formulated as binary variables, the UC models are mixed-integer programs. [13] provides a comprehensive treatment of the state-of-the-art UC formulations, including a comparative computational study.

For assessing the impact of large-scale integration of VERs into power systems, we propose transitioning from traditional deterministic approaches to stochastic optimization for both UC and ED. Stochastic programming (SP) has played a prominent role to enable decision making under uncertainty in real-scale problems across many application domains including power systems [27]. In particular, the two-stage stochastic programs (2-SPs), including models with discrete first-stage variables, have gained acceptance of both the power systems research community as well as practitioners (see surveys by [30] for UC and [6] for ED). We will use such 2-SPs to model DA, ST and RT operations.

Typical UC formulations studied in the literature (such as [1, 13, 19]) are deterministic MIPs and do not include transmission constraints. In our study, we extend a variant of the UC model in [1] into a 2-SP with the commitment decisions in the first-stage along with minimum up/downtime requirements. The ED model in the second-stage is based on [8]. This formulation includes a linear objective function that captures production cost along with over-generation/load-shedding penalties, and constraints corresponding to generation capacities,
ramping, flow balance, linearized power flow (DC approximation), operating reserve utilization, bounds on bus angles, and line capacities.

For HA-ED, we use a 2-SP model where the first-stage is used to determine the generation levels of committed slow-ramp generators while the second-stage determines the utilization of committed operating reserves in response to realizations of uncertain renewable generation and demand. We refer the reader to [1] and [8] for the detailed descriptions and additional considerations in UC and ED models, respectively. Here we provide only high-level models with a particular focus on the interactions between various model instances inside our hierarchical framework.

Let \( x \) and \( y \) be the vector variables that model the generators’ on/off statuses and production levels, respectively, for the entire planning period (say, a week), and define \( z = (x, y) \). The subscript \( d \) (as in, \( x_d \)) is used to refer to the variables associated with the day-ahead generators. A subscript \( [t] \) (as in, \( x_{[t]} \)) is used to refer to the set of time indices which are within the planning horizon of a model when it is solved for the \( t \)th time. We use three such subscripts, \( [i] \), \( [j] \), and \( [k] \), corresponding to the DA-UC, ST-UC, and HA-ED models, respectively. The randomness associated with the renewable supplies and the demand is embodied in random vectors that evolve over time. We denote these random vectors as \( \xi_i \), \( \xi_j \), and \( \xi_k \), for the \( i \)th, \( k \)th, and \( j \)th instants of the DA-UC, ST-UC, and HA-ED models, respectively.

We begin by presenting the deterministic models used in the DHP framework. Given the above notation, for a given day \( i \), we define the DA-UC model as follows:

\[
\text{DA-UC} \left( z_{[0]}^* \ldots z_{[i-1]}^*; \xi_{[i]} \right) = \min_{x_{[i]}, y_{[i]}} f_{[i]}^d(x_{[i]}, y_{[i]}) \quad (1)
\]

subject to: \( (x_{[i]}, y_{[i]}) \in X_{[i]}^d \left( z_{[0]}^* \ldots z_{[i-1]}^*; \xi_{[i]} \right) \).

Above, the function DA-UC(\( \cdot \)) uses the history of the generators (i.e., \( z_{[0]}^* \ldots z_{[i-1]}^* \)) and a single forecast of the renewable supplies and the demand (denoted as \( \xi_{[i]} \)) to determine feasible commitment schedules for the DA generators. The feasible region of the model is denoted as \( X_{[i]}^d (\cdot) \), and the function \( f_{[i]}^d(\cdot) \) captures the combined commitment and dispatch costs. We refer to the optimal solution of this model as \( z_{d,[i]}^* = (x_{d,[i]}^*, y_{d,[i]}^*) \).

Using the DA decisions (i.e., \( z_{d,[i]}^* \)), the \( j \)th ST-UC model is formulated as follows:

\[
\text{ST-UC} \left( z_{[0]}^* \ldots z_{[j-1]}^*; z_{d,[j]}^*, \xi_{[j]} \right) = \min_{x_{[j]}, y_{[j]}} f_{[j]}^s(x_{[j]}, y_{[j]}) \quad (2a)
\]

subject to: \( (x_{[j]}, y_{[j]}) \in X_{[j]}^s \left( z_{[0]}^* \ldots z_{[j-1]}^*; \xi_{[j]} \right) \),

\[
x_{d,[j]} = x_{d,[j]}^*, \\
y_{d,[j]} - y_{d,[j]}^* \leq \epsilon_j. \quad (2b)
\]

The ST-UC(\( \cdot \)) and DA-UC(\( \cdot \)) are similar in nature, except for (2a) and (2b). The former ensures that the DA commitment decisions are respected in the ST-UC model for generators that participate only in the DA market, and the later allows for their generation levels to be updated only within a bound defined by the parameter \( \epsilon_j \). Such bounds are placed to avoid myopic solutions of ST models as they have a shorter horizon than the DA model. Generators that participate only in ST markets can be (de)committed and all generators’ output levels can be adjusted in compliance with the constraints defining the feasible set \( \mathcal{X}^s(\cdot) \).

Using all the commitment decisions \( x_{d,[k]}^* \) and generation levels \( y_{d,[k]}^* \) prescribed by higher levels
UC models, the HA-ED model is instantiated as shown below:

$$\text{ED} (z^*_{[0]} \cdots z^*_{[k-1]}, \tilde{\xi}[k]) = \min f_{[k]}(x[k], y[k])$$

subject to: 

$$x[k] = x^*[k],$$ (3a)
$$|y[k] - y^*[k]| \leq \epsilon_k.$$ (3b)

Since the dispatch decisions are fixed in (3a), the resulting model only has continuous decision variables. As in the case of ST-UC, the constraint (3b) ensures that the HA generation does not deviate beyond $\epsilon_k$ to overcome the myopic nature of HA-ED model resulting from shorter horizon when compared to UC models at higher levels of hierarchy.

The deterministic variants of models defined in (1), (2) and (3) use only a point forecast $\tilde{\xi}[\cdot]$ and the objective function is defined as the cost associated with both unit commitment decisions as well as dispatch under such a point forecast. The main distinction between the models used in the DHP hierarchy and SHP hierarchy is that the objective functions of the latter are defined with a deterministic first-stage cost and expected recourse (second-stage) cost as follows:

$$f_{[t]}(x, y) = g_{[t]}(x, y) + E[h_{[t]}(x, y, \tilde{\xi})]$$  
$$t = i, j, k.$$ (4)

Notice that the recourse value $h_{[t]}$ is the optimal value of a second-stage optimization model that is instantiated by the first-stage decisions $(x, y)$ and a realization of the random variable $\tilde{\xi}$.

### 2.2 Solution Methods

The deterministic UC and ED models are solved using MIP and LP algorithms available in off-the-shelf solvers. In the 2-SP model for UC, we use a finite set of scenarios to represent the uncertainty. Even with modest numbers of scenarios, the resulting deterministic equivalent models could be very large and cannot be handled by off-the-shelf solvers. Given that the second-stage programs can be decoupled by scenarios and are LPs, we use the L-shaped (also known as Benders decomposition) algorithm to solve the stochastic UC models [26]. The basic idea of the L-shaped method is to approximate the expectation in the first-stage objective function in (4) using affine functions that are obtained via exact (dual) solutions of all second-stage LPs. The first-stage master program is solved as a linear MIP that comprises of the original constraints $X[\cdot]$ and the affine lower bounding functions.

The 2-SP formulation of HA-ED has linear first- and second-stage programs. We solve these models using a sequential sampling method called regularized stochastic decomposition (SD) algorithm [11]. Like the L-shaped method, SD is also a cutting-plane method that builds outer-approximations of the first-stage objective function. However, unlike the L-shaped method (which uses a fixed finite set of scenarios), SD operates with a scenario set that grows over the course of the algorithm (and hence the classification as a sequential sampling method). This allows the algorithm to determine a sufficient number of scenarios to ensure statistical optimality while optimization is being carried out concurrently (see [9] for details). While such a feature is desirable for SPs, there is a lack of such algorithms for models with discrete decision variables. Hence, we do not use successive sampling methods for UC models.

The scenarios that constitute stochastic UC instances and those used within the SD algorithm are generated using two time-series simulators, one for solar and another one for wind generators. The simulators are based on a vector auto-regression (VAR) model that captures temporal and spatial correlation of the stochastic processes governing generator outputs. A separate VAR model is estimated for each level of the hierarchy using the forecast time series in the NREL118 dataset. Subsequently, scenarios for optimization are simulated at their respective timescales using these prediction models (see [7] for a similar application).
3 Experimental Study

We conduct our experiments with the NREL118 dataset [20] that was introduced by the National Renewable Energy Laboratory for large-scale VER integration studies, such as the one undertaken in this paper. The topology of this system is based on the IEEE118 dataset which is widely recognized as a reasonable academic prototype. The NREL118 instance contains 327 generators (75 solar and 17 wind), 118 buses, and 186 transmission lines, along with forecasts and real-time outputs of renewable generators and demand. This dataset has a power system that is rich in solar, wind, and hydro resources, and may be consider futuristic/progressive.

We assess three factors that have significant impact on power system operations. These are solar and wind penetration, reserve requirements, and the planning strategy adopted for handling the UC and ED problems. By varying these factors, we analyze their impact on certain reliability metrics, as well as economic, and environmental ones, such as unmet demand, operating costs, and GHG emissions. In Table 1, we summarize the values considered for these factors in our experiments. We use a three letter identifier to recognize the type of optimization model (Deterministic or Stochastic) employed at the three planning levels in the hierarchy. Following this notation, the DDD setting is the benchmark planning framework (i.e., DHP), whereas both DDS and SDS can be considered as examples of SHP framework.

<table>
<thead>
<tr>
<th>Category</th>
<th>Label</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Solar &amp; Wind Integration</td>
<td>Low SW</td>
<td>Solar &amp; wind outputs as provided in the NREL118 dataset.</td>
</tr>
<tr>
<td></td>
<td>Med.</td>
<td>Twice the original values.</td>
</tr>
<tr>
<td></td>
<td>High SW</td>
<td>Thrice the original values.</td>
</tr>
<tr>
<td>Reserve Requirements</td>
<td>Very</td>
<td>5% for UCs, 1.25% for ED.</td>
</tr>
<tr>
<td></td>
<td>Low:</td>
<td>10% for UCs, 2.5% for ED.</td>
</tr>
<tr>
<td></td>
<td>Med.</td>
<td>15% for UCs, 5% for ED.</td>
</tr>
<tr>
<td></td>
<td>High:</td>
<td>20% for UCs, 10% for ED.</td>
</tr>
<tr>
<td>Planning Setting</td>
<td>DDD:</td>
<td>Deterministic DA-UC, ST-UC, ED.</td>
</tr>
<tr>
<td></td>
<td>DDS:</td>
<td>Det. DA-UC, ST-UC; stochastic ED.</td>
</tr>
<tr>
<td></td>
<td>SDS:</td>
<td>Det. ST-UC; stochastic DA-UC, ED.</td>
</tr>
</tbody>
</table>

Evaluations of the hierarchical frameworks are carried out in a rolling horizon manner. While the simulated scenarios from VAR models are used for optimization, the evaluations are carried using the actual observations (also available in the NREL118 dataset) made at every 15 minutes over a time-span of 7 days. In particular, the actual observations are used to instantiate the first-stage programs. Note that both the deterministic as well as stochastic frameworks are evaluated on the same actual observation time series. In what follows, we present the results obtained from these evaluations.

3.1 Reliability Impact

Significant amounts of unmet demand revealed in the planning process may potentially result into actual blackouts with damaging economic consequences for customers. Due to its importance to the ISOs and customers, we start our discussion with an illustration of average and maximum unmet demand values in Table 2.

In general, we notice higher unmet demand values when more solar and wind resources
introduced into the system. More conservative reserve requirements substantially reduce these values, but, possibly, comes with additional economic cost. On the other hand, adopting stochastic planning approaches into the modeling framework can zero out unmet demand, even at less conservative reserve requirements. For instance, to completely eliminate unmet demand from the planning process, DDD, DDS, and SDS necessitate high, medium, and low reserve requirements, respectively, under Medium SW and High SW settings. This observation supports the use of stochastic planning approaches to accommodate the variability of VERs, and reduce reliance on (manually-imposed) reserve restrictions. More importantly, it suggests the possibility of a more economical way of operating the system.

During our planning process, certain fast-ramping generators can be committed by the ST-UC problems to recover from unexpected supply shortages during the day. We evaluate the reliance on ST-UC problems by looking at the percentage of time that these generators were active (see Table 3). We observe a consistent trend where the DDD setting heavily relies on ST-UC problems to maintain reliability. In contrast, DDS and SDS substantially reduces these requirements even under higher renewable-integration settings.

Fig. 3 shows the average amounts of over-generation (by conventional generators) estimated under all settings. We observe the smallest amounts under the DDD setting. This is not surprising as it would never be optimal to over-produce in a deterministic optimization model provided that ramping capabilities are sufficient to cover ramping needs within the model’s horizon. In contrast, stochastic optimization (i.e., DDS and SDS) compensates for the variability in future time periods by over-generating in significantly larger amounts, thereby preventing situations where upwards-ramping capabilities may not be sufficient under certain settings.

In terms of solar and wind curtailment, Fig. 4 shows a significant trend where higher renewable integration leads to substantial amounts of curtailment, providing support to the need for energy storage. In addition, we still observe that both DDS and SDS leads to slightly more curtailment than that in DDD.
Fig. 3 illustrates intra-day generation profiles under DDD and SDS settings. Notice that the duck-chart is clearly visible. Another phenomenon to notice is that unmet demand, over-generation, and renewable curtailment may all occur simultaneously (at different buses), and the former two typically occur at day-time, when solar generators are active. As seen from the figure, SDS leads to more over-generation but reduces unmet demand from 16.9 MW to 0.7 MW. Furthermore, we observe higher variability in hydro-based generation under SDS (coefficient of variation of hydro-based generation is 0.13 in SDS vs. 0.05 in DDD). Hydro generators have better ramping capabilities, which makes them suitable for accommodating uncertainty. SDS naturally leverages this fact.

Fig. 4 shows the average curtailed solar and wind energy.

3.2 Economic Impact

Fig. 6 demonstrates the average daily generation costs recorded in our experiments\(^1\). In line with expectations, increased renewable integration leads to lower costs whereas increased reserve

\(^1\)The total operating costs will additionally include the penalty for load curtailment which is not presented in this figure.
requirements have the opposite effect.

Figure 6: Average daily generation cost of the power system under different reserve requirements and operations planning strategies.

We next turn our focus to the minimum reserve requirements levels at which the network demand is seamlessly fulfilled (in other works, no unmet demand is observed). Fig. 4 illustrates the daily operating costs corresponding to the minimum reserve requirements that must be set at each level of the hierarchy in order to ensure zero unmet demand. The figure indicates that, with stochastic optimization, reserve requirements can be loosened as the models are able to dynamically adjust production levels by accounting for uncertainty in the future. As a result, operating cost of the network can be reduced by up to 10.4% (e.g., compare $11.23M with DDD to $10.06M with SDS, under high renewable integration).

Table 4: Average daily operating cost of the power system corresponding to the minimum reserve requirements leading to zero unmet demand (in million $; Reserve requirements in paranthesis).

<table>
<thead>
<tr>
<th></th>
<th>DDD</th>
<th>DDS</th>
<th>SDS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low SW</td>
<td>12.42 (Med.)</td>
<td>11.56 (Low)</td>
<td>11.60 (Low)</td>
</tr>
<tr>
<td>Med. SW</td>
<td>12.11 (High)</td>
<td>11.00 (Med.)</td>
<td>10.66 (Low)</td>
</tr>
<tr>
<td>High SW</td>
<td>11.23 (High)</td>
<td>10.34 (Med.)</td>
<td>10.06 (Low)</td>
</tr>
</tbody>
</table>

3.3 Environmental Impact

To assess the environmental impact of operating the power system, we estimate the daily GHG emissions using the recorded generation amounts and mixes. Analogous to Fig. 4, Fig. 7 demonstrates daily CO$_2$ emission under the minimum reserve requirements that lead to zero unmet demand. Similar observations were made for the NO$_x$ and SO$_2$ emissions.

Figure 7: Average daily CO$_2$ emissions of the power system corresponding to the minimum reserve requirements leading to zero unmet demand (reserve requirements are noted on top of the bars).

We have two observations. First, in the experimented power system, higher renewable integration leads to lower levels of CO$_2$ emissions. While this sounds intuitive, opponents to this intuition typically suggest that the duck-chart phenomenon (i.e., insufficient ramping capabilities, volatility of renewables, and the resulting over-generation) could actually lead to more emissions. Our experiments confirm that this is not the case for power systems with
similar characteristics. Second, while stochastic modeling (i.e., DDS, SDS) leads to more over-generation and renewable curtailment (see Fig. 3-4), their impact can largely be reversed by the lower reserve requirements necessary to achieve the same level of reliability.

4 Discussion and Conclusions

We presented an SHP framework for power systems with large-scale VER penetration. While the call for a framework comprising of stochastic dynamic problems evolving at different timescales have been made before (e.g., [12]), this is the first study to conduct comprehensive computational experiments on such a framework. Our framework captures the operations and their interactions across day-ahead, short-term and hour-ahead timescales.

Our experiments indicate that the SHP framework overcomes many of the shortcomings of the DHP approach that is currently in practice. We observed that the SHP framework typically outperforms DHP in terms of reliability: Even at lower levels of reserve requirements, SHP is more effective in eliminating the unmet demand from the planning process. Moreover, with SHP, reliance on ST-UC problems (to avoid unmet demand) reduces. On the other hand, the SHP framework is more conservative and leads to more conventional over-generation and renewable curtailment, which can be mitigated by introducing storage resources to the grid. Finally, we observed that being able to operate reliably at lower levels of reserve requirements can mitigate excessive over-generation and renewable curtailment, as well as reduce the operating costs and GHG emissions.

The challenges associated with meeting ambitious renewable portfolio standards set in light of climate change concerns can be addressed principally through (i) efficient generator designs and power electronics, (ii) market designs, and (iii) optimization software used in planning and operations. In order to “tame the duck”, advances along all these three fronts will be critical. Efforts in this paper lay the groundwork for addressing (iii) through the SHP framework and the use of stochastic optimization tools. Our results are encouraging and point to the next steps that must involve experiments with actual ISO data. This will be undertaken as part of our future research endeavours.

References


