

Solution:

a) Given the anatomical dimensions and masses, determine forces F_L and F_R at the gymnast's hands. Solve the problem symbolically first, then numerically, and show your work for each part.

Step 1: Write the equations of static equilibrium.

$$\begin{aligned}\sum F_x &= F_{breeze} \cdot (\text{body length}) - R_R - R_L \\ \sum F_y &= -(2 \cdot m_{leg} + m_{torso})g + F_L + F_R = 0\end{aligned}$$

Step 2: Write the moments about the right hand, making sure to include the contribution of the left leg due to its abduction angle.

$$\begin{aligned}\sum M_R &= -(m_{torso} \cdot g \cdot l_{clav}) + (F_L \cdot 2l_{clav}) - (m_{leg} \cdot g(l_{clav} + l_{hip} + l_{knee} \sin(45))) \\ &\quad - (m_{leg} \cdot g(l_{clav} - l_{hip})) - \frac{1}{2}F_{breeze} \cdot (l_{arm} + l_{torso} + l_{leg})^2 = 0\end{aligned}$$

Step 3: Then solve for F_L .

$$F_L = \left[(m_{torso} \cdot g \cdot l_{clav}) + (m_{leg} \cdot g(l_{clav} + l_{hip} + l_{knee} \sin(45))) + (m_{leg} \cdot g(l_{clav} - l_{hip})) + \frac{1}{2}F_{breeze} \cdot (l_{arm} + l_{torso} + l_{leg})^2 \right] / 2l_{clav}$$

With $g = 10 \text{ m/s}^2$,

$$\gg F_L = 431.18 \text{ N}$$

With $g = 9.8 \text{ m/s}^2$,

$$\gg F_L = 422.83 \text{ N}$$

Step 4: Now, use the static equilibrium equation for force in the y -direction to solve for F_R .

$$\sum F_y = -(2 \cdot m_{leg} + m_{torso})g + F_L + F_R = 0$$

$$F_R = (2 \cdot m_{leg} + m_{torso})g - F_L$$

With $g = 10 \text{ m/s}^2$,

$$\gg F_R = 168.82 \text{ N}$$

With $g = 9.8 \text{ m/s}^2$,

$$\gg F_R = 165.17 \text{ N}$$