Using Electrical Density Gauges for Field Compaction Control

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ABSTRACT

Compacted soil is a vital element in the construction of any civil engineering project. Measurements of in-situ soil density and moisture content are commonly used in the residential, commercial, and transportation industries to control the process of soil compaction. Various methods currently exist to monitor compaction in soils for construction projects. The nuclear density gauge is currently the most commonly utilized test device for this purpose; however, there are strict regulations with respect to the handling, transport, and storage of this device because it contains radioactive material. A relatively new non-nuclear alternative is the electrical density gauge (EDG), which uses a series of electrical measurements in conjunction with calibrated soil models to infer in-situ soil density and moisture content. Two approaches currently exist for building soil models with the electrical density gauge: the first is calibration with in-situ measurements of density and water content provided by the nuclear density gauge, sand cone test, or an equivalent in-situ density test, and the second is calibration with “large mold” Proctor-type tests.

In this study, both calibration methods were evaluated. Additionally, field compaction conditions were simulated in a “large” box where EDG tests and three common in-situ density tests (nuclear density gauge, sand cone, and drive cylinder) were performed to provide comparative results. The findings from this study provide
guidance for interpreting the results from future electrical density gauge studies, and are useful for engineers that may be considering the use of this technology for compaction control.
Chapter 1

INTRODUCTION

Compacted soil is a vital element in the construction of highways, airports, buildings, sewers, and bridges. Therefore, measurements of in-situ soil density and moisture content are commonly used to control the process of soil compaction in the construction industry. Various methods currently exist to monitor compaction in soils.

In the State of Delaware the current approach that is used compares measurements of in situ soil density and moisture content with measurements of soil density and moisture content that are obtained from a standard-energy compaction test approach (1-Point Standard Proctor Compaction). Measurements of in situ soil density and moisture content are typically obtained via a nuclear density gauge (NDG). The results of NDG tests exhibit significant scatter when compared to previous in-situ density test standards (e.g. sand cone tests, rubber balloon tests, etc). Despite these characteristics of the test, the nuclear density gauge has become the accepted industry standard for quality control of soil compaction. This is because tests can be taken rapidly and are much easier to perform than other density-based quality control tests.

In addition to the inherent inaccuracies of NDG testing, there are significant regulatory compliance issues that are present when dealing with NDG test equipment. The NDG contains radioactive material, which is heavily regulated by the Nuclear Regulatory Council. This regulation requires strict protection standards for employees working with the equipment. Particularly for large-scale NDG operations, such as those at the Delaware DOT, these nuclear regulatory issues can present a significant obstacle to
operations, and compliance can be difficult. Thus, using a non-nuclear based approach for in-situ density testing has become more desirable.

Recent technological innovations currently provide many alternative opportunities to use non-nuclear technology for compaction control. Some non-nuclear methods to monitor soil moisture currently exist and methods to measure density for geotechnical engineering applications are being developed as well. Time domain reflectometry (TDR), capacitance sensors, and electrical impedance spectroscopy (EIS) are some of the methods that are currently utilized.

A relatively new non-nuclear alternative is the electrical density gauge (EDG), which uses a series of electrical measurements in conjunction with calibrated soil models to infer in-situ soil density and moisture content. Two approaches currently exist for building soil models with the electrical density gauge: the first is calibration with in-situ measurements of density and water content provided by the nuclear density gauge or the sand cone test, and the second is calibration with “large mold” Proctor-type tests.

In order to evaluate the accuracy of the EDG and to assess whether the instrument can and should be implemented for the Delaware Department of Transportation, two experimental studies have been performed. In the first phase of this project, in-situ measurements of soil on active construction projects were taken. After considerable time trying to get the necessary data on active construction projects to fairly assess the EDG, it was determined that this was not feasible. The inability to control moisture content and temperature of the soil in the field, as well as the demands of contractors to not slow down progress on projects led to a second
experimental study. Large box testing of soil in conjunction with large mold testing was performed to acquire the necessary data to evaluate the accuracy of the EDG.

The goal of this thesis is to present the results from the aforementioned research project, providing a detailed description of the activities that were performed from the beginning to the end of this project. In Chapter 2, a summary of relevant literature that was reviewed will be presented. In Chapter 3, the operating principles and basic fundamentals of the EDG will be explained. In Chapter 4, the initial experimental field studies that were performed will be explained in detail. Results from the experimental studies will be presented and explained in Chapter 4 as well. In Chapter 5, “large mold” calibration procedures and testing results will be explained in detail. Experimental studies simulating field conditions undertaken in “large box” tests will be presented and explained in Chapter 6. In Chapter 7, the most significant conclusions from this research project will be presented and recommendations for future research in this area will be provided as well. The findings from this research project will provide guidance for interpreting the results from future electrical density gauge studies, and are useful for engineers that may be considering the use of this technology for compaction control.
Chapter 2

LITERATURE REVIEW

2.1 In-Situ Moisture Content and Density Testing

The compaction of soil in embankments, subbase or base course layers is one of the most important aspects of construction of highways, buildings, sewers, bridges, and airports. In order to ensure that soil is placed as specified and with uniformity, frequent testing of the compacted soil is necessary. Using conventional quality assurance / quality control (QA/QC) procedures, this testing typically requires that the in-place dry density (or dry unit weight) of the soil be measured along with the soil moisture content (e.g., DelDOT 2001). The measured in situ density is compared to a specified reference value, which is typically determined as a percentage of the standard (or modified) Proctor density value (ASTM D 698, ASTM D 1557). The measured in situ moisture content is typically required to be within a specified range of the optimum moisture content (e.g., ± 2%), which is determined as a percentage of the standard (or modified) Proctor optimum moisture content value (e.g., DelDOT 2001).

The standard approach used for controlling the degree of compaction in soil is to measure the in situ dry density (or dry unit weight) and moisture content of the compacted soil at random locations throughout the area of construction. The measured values are then compared with acceptable ranges of dry unit weight and moisture content for that specific material. Two methods to specify a target range for the dry unit weight and moisture content exist.
The first method is the 5-pt Proctor test, in which five or more specimens are compacted in a uniform, controlled manner at different moisture contents. After the compaction tests are performed, the moisture contents and dry unit weights of the specimens are determined. A compaction curve derived from the measured data is then plotted that shows the relationship between the measured dry unit weight and the water content. From this curve, a maximum dry unit weight can be determined, and this value and the corresponding optimum moisture content for compaction are recorded. In general, two types of 5-point Proctor tests are commonly used; the standard Proctor test (ASTM D 698) and the modified Proctor test (ASTM D 1557).

The second method is the 1-pt Proctor test (AASHTO T 272) in which only one compaction test is performed and the resulting dry unit weight and moisture content are used with a group of compaction curves to determine the optimum moisture content and maximum dry unit weight. The group of curves that are used for a given soil are developed over time, based on long-term experience with 5-point Proctor tests for a given borrow material. Consequently, it is necessary to have a separate group of curves for each material type that is placed.

Values of dry unit weight obtained from in situ measurements on a compacted lift are then divided by the maximum dry unit weight that is achieved from either the 1-point Proctor or 5-point Proctor, providing the relative compaction (RC), which is also commonly referred to as the degree of compaction. The measured field moisture content ($\omega_{\text{field}}$) is compared with the optimum moisture content ($\omega_{\text{opt}}$) obtained from either the 1-point Proctor or 5-point Proctor. Both the relative compaction and moisture content must meet the corresponding acceptance criteria (e.g. $\text{RC} \geq 95\%$ and $\omega_{\text{opt}} - 2\% \leq \omega_{\text{field}} \leq \omega_{\text{opt}} + 2\%$ (DelDOT 2001), otherwise compaction of
the lift that was placed in the field must be repeated. As noted above, the most
commonly used methods for compaction control use measurements of in situ soil
density and moisture content to assess the effectiveness of the compaction process.
The most common in situ tests that are utilized with this approach are the nuclear
density gauge test (ASTM D 6938), the sand cone test (ASTM D 1556), and the rubber
balloon test (ASTM D 2167).

2.1.1 The Nuclear Density Gauge Test

The nuclear density gauge (Figure 2.1) is currently one of the most
commonly used devices to determine the in situ unit weight and water content of soil
(ASTM D 6938). Nuclear density gauges are relatively simple to use, determine soil
characteristics rapidly, and are relatively accurate (e.g., Randrup et al 2001).
However, there are strict regulations with respect to the handling, transport, and
storage of these devices because they contain radioactive material. This has led to
ongoing research into non-nuclear alternatives for speedy determination of in situ unit
weight and water content of compacted soils (e.g., Electrical Density Gauge, Soil
Density Gauge (Transtech)).

Figure 2.1 Troxler 3440 Nuclear Density Gauge
The nuclear density gauge is a measuring device that is used to indirectly measure in-situ dry density and moisture content of aggregate and soil layers by means of radioactive particles emitted into the ground. A typical nuclear density gauge consists of a 20 cm or 30 cm (8 or 12-in.) retractable rod, a Geiger-Muller detector, and a display screen. The nuclear gauge can operate in two different ways, the backscatter mode and the direct transmission mode (Figure 2.2). In the backscatter mode, the nuclear source and probe are both located on the ground surface. When operating in direct transmission mode, a retractable rod with a nuclear source is placed in the ground, while the detector remains located on the ground surface. The direct transmission mode is considered more accurate and is always used on soil density tests. Backscatter mode is mostly used for testing asphalt, concrete, and materials that cannot be penetrated easily such as densely compacted stone.

**Figure 2.2** Nuclear Density Gauge Transmission Modes (modified from Troxler Model 3430 Manual of Operation and Instruction, 1990-2006)
In order to measure in situ unit weight, an isotope source, usually Cesium 137, is fixed upon the end of the retractable rod, where it continuously emits photons and gamma rays. The gamma rays interact with electrons in the base material and are counted when they return to the Geiger-Muller detector. The lower the number of photons measured by the detector, the higher the density of the material being tested.

For measurement of in situ moisture content, neutrons emitted by the radioactive source are thermalized by contact with hydrogen atoms. Thermalization is the loss of kinetic energy to the degree that further collisions with hydrogen or other materials will not continue to slow the neutron. Since the neutron detector in the nuclear density gauge is sensitive only to thermalized neutrons, the returning neutron count obtained by the detector is directly proportional to the hydrogen count and subsequently to the water content of the material. Moisture measurements typically utilize Americium-241:Beryllium as a source neutron emitter in conjunction with a neutron detector referred to as an He-3 tube, which is used due to its high sensitivity to thermalized neutrons and insensitivity to fast neutrons. When the gauge is placed on an area to be measured, the neutrons emitted by the Americium 241: Beryllium source are thermalized by hydrogen molecules contained in the measured material and these thermalized neutrons are detected by the He-3 tube and displayed as the moisture count.

Nuclear density gauges undergo an initial calibration every day using a reference block. The reference block is made of polyethylene due to the presence of hydrogen in the molecular structure of the material. The hydrogen molecules in the block simulate a specific amount of water, which is what the gauge detects during calibration testing. Since the polyethylene block’s molecular structure does not change
and is very consistent, it is used for the daily standard calibration count. Standardization involves recording four readings on a reference block, and computing their mean value. Then a comparison to the current standardization count is performed, and if it falls with the acceptable limits outlined in ASTM D 6938, the gauge is acceptable to use. This process is done to ensure that the gauge is performing accurately and consistently from day to day.

2.1.2 The Sand Cone Test

The sand cone test is a sand replacement method for determining the in situ unit weight or density of natural or compacted soil (ASTM D 1556). This method is limited to materials with a maximum particle size of 5.1 cm (2 in) and is applicable for soils without appreciable amounts of rock or coarse materials in excess of 38 mm (1.5 in.) in diameter as well. This test method is not recommended for soils that are soft and crumble easily or in conditions where water can seep into the hand excavated hole (ASTM D 1556).

Figure 2.3 Sand Cone Apparatus
To perform a sand cone test, a hole is excavated by hand with a small shovel in the area where the soil has been compacted. The dry weight of the soil is obtained by determining the weight of the moist soil that is excavated from the hole and its moisture content. The moisture content is typically determined by standard oven-drying procedures, or can be done in the field with a hot plate or microwave (e.g., ASTM D 2216, ASTM D 4643). The volume of the excavated hole is determined by filling the hole with a uniform sand. The sand cone apparatus (see Figure 2.3) is used to fill the hole and is weighed before and after the placement of sand to determine the volume of sand that is in the hole. The in situ dry unit weight of the soil is then calculated by dividing the dry weight of the soil by the volume of the hole.

2.1.3 The Rubber Balloon Test

The rubber balloon test for in-situ soil density testing (ASTM D 2167) is very similar in principle to the sand cone method. As with the sand cone test, a hole is excavated by hand with a small shovel in the desired location and the soil removed from the hole is stored in an air-tight container for weight and moisture content determination. An apparatus consisting of a graduated cylinder and rubber balloon (see Figure 2.4) is used to measure the volume of fluid that is needed to fill the excavated hole.
This test method can be used to determine the in-place density and unit weight of natural soil deposits, soil-aggregate mixtures, or other similar materials. The use of this test method is limited to soil with low water contents and is not recommended for soils that are soft or deform easily. Certain soils may undergo a volume change when pressure is applied during testing. Soils with crushed rock or jagged edges are not suitable for this test because they may puncture the rubber balloon membrane as well.

2.1.4 Time Domain Reflectometry (TDR)

The time domain reflectometry (TDR) method of monitoring subgrade water content was introduced in the area of pavement engineering around 1989 (Neiber and Baker 1989). A TDR measurement system typically includes a transmission line, a coaxial connecting cable, a TDR instrument, and probes inserted in the soil. A typical TDR setup in the field is shown in Figure 2.5.
The TDR method measures the velocity of an electromagnetic wave travelling in a transmission line. The velocity \( v \) of the wave running through the line is related to the apparent dielectric constant \( K_a \) of the insulating medium between the conductors of the transmission line (Krauss 1984). The associated relationship is as follows (Equation 2.1):

\[
v = \frac{c}{\sqrt{K_a}}
\]

where \( c \) is the velocity of light in a vacuum and \( K_a \) is given by Equation 2.2

\[
K_a = \frac{K'}{2} \left[ 1 + \sqrt{1 + \left( \frac{K'' + \frac{\sigma_d}{\omega \varepsilon_0}}{K'} \right)^2} \right]
\]
where \( \omega \) is the angular frequency, \( \varepsilon_0 \) is the permittivity of a vacuum, \( K' \) and \( K'' \) are the real and imaginary parts of the complex dielectric constant, and \( \sigma_{dc} \) is the direct current electrical conductivity.

When used in soil science and geotechnical engineering applications, the TDR probe is the transmission line and the insulating medium is the soil. The TDR instrument sends a step voltage pulse through the coaxial cable and when the signal reaches the beginning of the probe, part of the pulse is reflected back to the TDR instrument. This occurs because of a mismatch in impedance between the coaxial cable and the soil probe. When the remaining portion of the signal reaches the end of the probe, a reflection of the signal occurs again. Both reflections cause two discontinuities in the signal which is recorded by the TDR instrument, and the time difference between these two discontinuities is the time \( (t) \) required by the signal to travel twice the length \( (L) \) of the probe in the soil. Therefore the wave propagation velocity in the soil is represented by Equation 2.3:

\[
v = \frac{2L}{t} \tag{2.3}
\]

The dielectric constant of the soil is represented by Equation 2.4:

\[
K_a = \left( \frac{ct}{2L} \right)^2 \tag{2.4}
\]
Topp et al. (1980) developed an empirical relationship that is based on a correlation between the dielectric constant of a soil and its volumetric water content (\(\theta\)). The following equation describes this relationship (Equation 2.5, Topp et al. 1980):

\[
\theta = -0.053 + 2.92 \times 10^{-2} K_a - 5.5 \times 10^{-4} K_a^2 + 4.3 \times 10^{-6} K_a^3
\]  

(2.5)

The equation above can be used for all types of soils, but more specific equations for different soil types exist as well. For geotechnical engineering applications, gravimetric water content is more commonly used. The following relationship exists between volumetric and gravimetric water content (Equation 2.6):

\[
w = \frac{\theta \rho_w}{\rho_d}
\]  

(2.6)

where \(\rho_d\) and \(\rho_w\) are the dry density of soil and water respectively.

Siddiqui and Drnevich (1995) have been able to extend TDR to geotechnical applications. They developed a calibration equation relating soil gravimetric water content and dry density to apparent dielectric constant. With the use of their calibration equation, they designed a procedure that uses a TDR approach for geotechnical compaction control. First, a laboratory calibration is performed to obtain constants that are dependent on soil type for further field measurements. Calibration is performed in conjunction with compaction tests to create compaction quality control criteria. The procedure in the field consists of two TDR tests. One TDR test is taken with a probe with four coaxially configured spikes driven into the soil, and one test is conducted in a compaction mold on the same soil that was immediately excavated from within the four spikes and hand compacted into the mold. The gravimetric water
content for both tests, the apparent dielectric constants from both TDR readings, and the measured total density of the soil in the mold are used to calculate soil water content and dry density. Laboratory and field evaluations indicate the method has sufficient accuracy for geotechnical purposes (Lin 1999; Siddiqui et al. 2000; Drnevich et al. 2001a, 2002). ASTM D 6780 currently exists to govern the use of TDR for typical geotechnical engineering compaction control applications.

2.1.5 Capacitance Sensors

Capacitance sensors or dielectric sensors (e.g., Figure 2.6) use capacitance to measure the dielectric permittivity of materials (e.g., Kelleners et al. 2004). Capacitance sensors are configured similarly to neutron probes in which a tube made of PVC is installed and inserted into the soil (Kelleners et al 2004). The probe inside the tube is made up of a sensing head that is located at a fixed depth. Within the sensing head are an oscillator circuit, an annular electrode, and a fringe-effect capacitor, which are used in determining the dielectric constant of the soil. The capacitance sensors are made up of two metal rings that are attached to a circuit board at a specific distance from the top of the PVC access tube. The metal rings form the plates of the capacitor and are connected to an oscillator circuit. An electrical field is generated by the oscillator circuit between the two metal rings and flows from the walls of the access tube into the soil. The oscillator circuit and the capacitor form a circuit and detect changes in the dielectric constant of the material within the access tube by changing the operating frequency. Most capacitance sensors are designed to oscillate in excess of 100 MHz inside the access tube, and the output of the sensor is the frequency response of the soil’s capacitance due to the moisture content in the soil.
Figure 2.6  Capacitance Sensor (modified from Schwank et al. 2006)

The resonant frequency of an oscillator circuit that includes the soil is represented by the following equation (Equation 2.7) (Kelleners et al. 2004, Fares et al. 2007):

\[
F = \left( \frac{2\pi \sqrt{L \left( C_s + \frac{C_a C_m}{C_p + C_m} \right)}}{C_p + C_m + C_m} \right)^{-1}
\]  
(2.7)

where \( C_m \), \( C_p \), and \( C_s \) are the capacitances of the medium, plastic access tube, and capacitance due to stray electric fields, respectively. The observed frequency is used to determine the scaled frequency, \( SF \), by the following equation (Equation 2.8):

\[
SF = \frac{F_a - F_s}{F_a - F_w}
\]  
(2.8)
where $F_a$, $F_w$, $F_s$, are the frequency readings of the sensor inside the plastic tube of air, water, and soil respectively at room temperature.

The value of the scaled frequency varies between 0 and 1 depending on the ratio of air to water in the soil medium. The scaled frequency value is the used in a calibration equation to estimate the soil water content. The following equation (Equation 2.9) is one empirical equation that has been developed that can be used to estimate the volumetric water content using a capacitance sensor (Fares et al. 2007):

$$
\theta_v = \left( \frac{SF - 0.02852}{0.1957} \right)^{0.404}
$$

(Equation 2.9)

Currently, capacitance sensors are being tested and used mainly by soil scientists to monitor and measure the moisture content of soils for agricultural purposes.

2.1.6 Electrical Impedance Spectroscopy

The Soil Density Gauge (SDG) manufactured by Transtech Systems employs Electrical Impedance Spectroscopy (EIS) to infer the density and moisture content of soil. EIS measures the dielectric properties of a medium as a function of frequency. EIS theory is based on the interaction of an external electrical field with the electric dipole moment of the medium (Gamache et al. 2009). This method measures the impedance of a medium over a range of frequencies. The frequency response of the system is captured and various relationships can be deciphered from these responses.
In soil, the electromagnetic response is primarily determined by the dielectric properties of the materials in the soil. The non-uniformity of the soil combined with interfacial effects between polar water molecules and soil solids results in a complex electrical response. The three primary polarization mechanisms in soil that contribute to this response are bound water polarization, double layer polarization, and the Maxwell-Wagner effect. Since water can be electrostatically bound to the soil matrix it contributes heavily to the measured complex electrical response. The separation of cations and anions, which leads to double layer polarization, occurs more frequently in soils with large clay fractions. In addition, the Maxwell-Wagner effect is the most critical phenomenon that affects the low radio frequency dielectric spectrum of soils. The Maxwell-Wagner effect depends on the differences in dielectric properties of the soil elements resulting from the distribution of non-conducting and conducting areas in the soil matrix (Gamache et al. 2009).

TransTech Systems has found that well-graded sandy soils suitable for engineering fill exhibit a single Maxwell-Wagner relaxation in the 1-10 MHz range. In frequency ranges above this, the dielectric response is described by using empirically derived mixing equations in which the matrix bulk dielectric constant is proportional to the sum of the products of the volume fractions and dielectric constants of the soil elements. When soil undergoes compaction, the volume fraction of air is reduced and the volume fractions of soil and water are increased, which results in an increase in both the permittivity and conductivity of the soil (Gamache et al. 2009). Through detailed study, Transtech Systems has learned that certain characteristics of the impedance response in the Maxwell-Wagner portion of the spectrum can be used in a parametric inversion method to measure wet density and volumetric moisture
content (Gamache et al. 2009). Specific parameters in the impedance response contain moisture and density information and are converted to wet density and volumetric moisture content using simple regression analysis. In the current model, specific parameters related to soil type and gradations at each job site are used to adjust the standard laboratory calibration equations (Gamache et al. 2009).

2.2 Statistical Analyses of Standard In-Situ Density Tests

In order to have a better understanding of the accuracy and relative error of the most common in-situ soil density tests, a review of previously published test studies was performed.

2.2.1 Comparisons of Field Density Test Results (Kaderabek & Ferris 1979)

Kaderabek & Ferris (1979) describe the results from compaction control tests conducted during a large earthwork project in Georgia, where 6 test fill areas were constructed to investigate compaction procedures. Proctor tests were performed at each field density test location, as well as nuclear density tests and sand cone tests. At each test fill location either 24 or 30 nuclear density gauge tests and 24 or 30 sand cone tests were performed. Two different soil types were used in the construction of the test fill areas: Slightly silty slightly clayey fine to medium sand (SM) (Stockpile A-Test Fill Numbers 3, 4 & 5), and slightly silty fine to medium sand (SM-SW) (Stockpile C-Test Fill Numbers 1, 2 & 6) (Kaderabek & Ferris 1979).

In order to evaluate the relative agreement of testing parameters for both the nuclear density gauge and sand cone tests, the standard deviation of each type of test at each test fill location were compared. Figures 2.7 through 2.9 show the standard deviation of moist unit weight, moisture content, and relative compaction for
the NDG and SC tests that were performed at all test fill locations. The standard deviation of moist unit weight test values for the NDG is greater than the standard deviation of the SC method values at 5 of the 6 test fill locations. In terms of moisture content, the NDG standard deviation is nearly double the standard deviation of the SC method (oven dried). The standard deviation for relative degree of compaction is approximately equal for the nuclear density gauge and sand cone method. Table 2.1 and Table 2.2 list all the values that were used to generate the figures in this section.

The overall conclusion derived from this test study is that the sand cone method determines dry unit weight and moist unit weight that are consistently greater than the values measured by the nuclear density gauge. In addition, the moisture content values measured by the sand cone method (oven dried) are lower than the values determined by the nuclear density gauge. Also, the standard deviation of the nuclear density gauge when measuring moisture content is nearly double the standard deviation of the sand cone method (oven dried).
Figure 2.7  Moist Unit Weight Standard Deviation  
(Data from Kaderabek & Ferris, 1979)
Moisture Content Standard Deviation

- NDG: Mean + S.D.
- SC: Mean + S.D.
- NDG: Mean - S.D
- SC: Mean - S.D
- NDG: Mean
- SC: Mean

Figure 2.8  Moisture Content Standard Deviation
(Data from Kaderabek & Ferris, 1979)
Figure 2.9  Relative Compaction Standard Deviation  
(Data from Kaderabek & Ferris, 1979)
Table 2.1  Nuclear Density Gauge data (Kaderabek & Ferris 1979)

<table>
<thead>
<tr>
<th>Test Fill Number</th>
<th>Moist Unit Weight (pcf)</th>
<th>S.D.</th>
<th>Moisture Content (%)</th>
<th>S.D.</th>
<th>Relative Compaction (%)</th>
<th>S.D.</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 (24 tests)</td>
<td>128.30</td>
<td>2.40</td>
<td>12.60</td>
<td>1.30</td>
<td>93.50</td>
<td>1.90</td>
</tr>
<tr>
<td>4 (24 Tests)</td>
<td>127.70</td>
<td>1.80</td>
<td>12.80</td>
<td>1.70</td>
<td>93.00</td>
<td>1.80</td>
</tr>
<tr>
<td>5 (30 Tests)</td>
<td>124.60</td>
<td>3.00</td>
<td>13.20</td>
<td>2.10</td>
<td>90.40</td>
<td>2.80</td>
</tr>
<tr>
<td>1 (30 Tests)</td>
<td>125.60</td>
<td>3.00</td>
<td>10.70</td>
<td>2.10</td>
<td>98.90</td>
<td>2.30</td>
</tr>
<tr>
<td>2 (24 Tests)</td>
<td>127.10</td>
<td>2.50</td>
<td>10.50</td>
<td>3.40</td>
<td>99.70</td>
<td>1.60</td>
</tr>
<tr>
<td>6 (30 Tests)</td>
<td>114.90</td>
<td>2.00</td>
<td>11.40</td>
<td>2.50</td>
<td>97.30</td>
<td>2.50</td>
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<td>Average</td>
<td></td>
<td>2.45</td>
<td></td>
<td>2.18</td>
<td></td>
<td>2.15</td>
</tr>
</tbody>
</table>

Table 2.2  Sand Cone Method data (Kaderabek & Ferris 1979)

<table>
<thead>
<tr>
<th>Test Fill Number</th>
<th>Moist Unit Weight (pcf)</th>
<th>S.D.</th>
<th>Moisture Content (%)</th>
<th>S.D.</th>
<th>Relative Compaction (%)</th>
<th>S.D.</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 (24 tests)</td>
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<td>3.10</td>
<td>10.40</td>
<td>0.70</td>
<td>97.90</td>
<td>2.10</td>
</tr>
<tr>
<td>4 (24 Tests)</td>
<td>132.90</td>
<td>1.90</td>
<td>9.80</td>
<td>0.80</td>
<td>99.30</td>
<td>1.60</td>
</tr>
<tr>
<td>5 (30 Tests)</td>
<td>129.70</td>
<td>2.90</td>
<td>9.40</td>
<td>1.00</td>
<td>97.30</td>
<td>2.10</td>
</tr>
<tr>
<td>1 (30 Tests)</td>
<td>128.10</td>
<td>3.20</td>
<td>8.60</td>
<td>1.50</td>
<td>102.80</td>
<td>1.80</td>
</tr>
<tr>
<td>2 (24 Tests)</td>
<td>127.50</td>
<td>4.20</td>
<td>9.00</td>
<td>1.80</td>
<td>103.90</td>
<td>2.30</td>
</tr>
<tr>
<td>6 (30 Tests)</td>
<td>120.70</td>
<td>1.30</td>
<td>8.10</td>
<td>1.70</td>
<td>105.40</td>
<td>2.00</td>
</tr>
<tr>
<td>Average</td>
<td></td>
<td>2.77</td>
<td></td>
<td>1.25</td>
<td></td>
<td>1.98</td>
</tr>
</tbody>
</table>
Comparative Accuracy of In-Situ Nuclear Density Testing (Ishai & Livneh 1983)

Ishai and Livneh (1983) performed a field study to assess field density testing approaches during the construction of the Etzion and Ouvda Airports in southern Israel in 1983. In order to evaluate the accuracy of the nuclear density gauges, Ishai & Livneh felt it was necessary to study the accuracy of the conventional sand-cone density test and oven-drying moisture test first.

Conventional sand-cone density and oven-drying moisture tests were performed on four road sections of the Tel Aviv-Haifa freeway on clay subgrade, sandstone subbase, and limestone-dolomite base courses. The following conclusions were determined from this initial study:

1) There is significant variability in field density and moisture content values due to the inherent variable nature of material, and due to human errors in measurement. Coefficients of variation were as high as 8% for density.

2) Comparisons between two testing operators showed that the criterion for maximum deviation in field density and moisture content were not fulfilled in 85% of the cases, signifying the effect of human errors in measurement on results.

After the initial study analyzing conventional density and moisture testing was performed, a second study was carried out. A test section of 24 meters by 45 meters was constructed in which the following tests were performed: two sand cone tests by two operators at the same time (Series A - 21 tests), two sand cone tests by two operators at different times (Series B - 18 tests), which were conducted not knowing in advance that a second test would be taken, and nuclear density gauge tests
that utilized the backscatter method (Series C - 18 tests). The following conclusions were determined from the second phase of this study:

1) Significant scatter in wet density results from sand cone tests were obtained, mainly caused by material variability, construction and human factors. The maximum coefficient of variation for wet density was 37%.

2) More variability was observed in Series A than in Series B. This occurred mainly because each operator knew that he would be checked by a second test and operator.

3) The accuracy of the sand cone and oven-drying method is not highly accurate, as many engineers typically assume. In addition, accuracy in the oven-drying test was found to be higher in granular material than that in fine-grained plastic materials.

The final phase of this study was aimed at evaluating the accuracy and repeatability of the nuclear density gauge. The following conclusions were determined from the final phase of this study:

1) The repeatability characteristics of the nuclear density gauge were very high. In most cases, the standard deviation for moist unit weight did not exceed 0.20 kN/m$^3$.

2) The repeatability characteristics of moisture content for the nuclear density gauge were still relatively high (e.g., their probability of deviating more than 0.16 kN/m$^3$ was between 2 and 67 percent); however, the observed repeatability was lower than that which was observed for the moist unit weight.
Ultimately, the final conclusions Ishai & Livneh determined from their study were:

1) The material presented in this study cannot lead to the conclusion that the nuclear method for density and moisture content is more accurate than the conventional tests, due to the fact that it is not possible to repeat a sand cone or oven-drying moisture test in the same exact location. This inherently leads to a natural variability due to material composition.

2) The repeatability characteristics of nuclear testing are very high and justify its practical usage. Also, it is suggested that three readings taken after rotating the gauge by 120° should be averaged for most accurate results.

2.2.3 Nuclear Density Gage Tests on Soils Containing Various Sized Aggregates (Gabr et. al. 1995)

Gabr et. al. (1995) conducted a testing program on soil samples containing varying amounts of pre-sized limestone aggregates in order to investigate the accuracy of the nuclear density gauge (NDG) in gravelly soils. In this study, test specimens of known density were compacted with a 10 kg weight from a height of 0.61 meters in a 0.56 x 0.71 x 0.58 meter (width, length, height) acrylic box. Eight (8) sand cone tests were performed on each box at various locations, and nuclear density tests were performed in the backscatter mode, and at various depths in the direct transmission mode. The major conclusions Gabr and his colleagues determined from this test study are the following:
1) Variability in density predicted by the NDG increased as aggregate size was increased. Also, NDG variability was less than sand cone tests due to the difficulty of running sand cone tests in soils containing aggregates.

2) Coefficient of determination ($R^2$) values between box values and nuclear values decreased from 0.92 for soil with small aggregate to 0.51 for soil with large aggregate.

3) Oven-drying provided accurate values for moisture content for all soils tested, and results from NDG tests had slightly lower correlation coefficients than those obtained using oven-drying.

4) Moisture content data from NDG tests resulted in coefficients of determination increasing with an increase in aggregate size, thus indicating that the NDG may not be affected by the presence of aggregate.

2.2.4 Evaluation of Nuclear Methods of Determining Surface In Situ Soil Water Content and Density (U.S. Army Engineer Waterways Experiment Station 1969)

The U.S. Army Engineer Waterways Experiment Station (WES) conducted a laboratory investigation to evaluate the accuracy and reliability of measuring water content and density by the backscatter and direct transmission nuclear methods. In this study, boxes (2 ft by 2 ft by 9 in.) were constructed, filled with uniformly compacted soil, and then weighed to determine actual average soil density values. Five soil types were selected for testing in order to approximate a range of possible construction materials: heavy clay (CH), lean clay (CL), sand (SP), clayey gravelly sand (SP-SC), and a well-graded crushed limestone. Each of the soils was tested at eight different densities and water contents, resulting in 40 samples. In addition, two accepted conventional methods for determining density in the field, the
sand cone and rubber balloon methods, were performed. Figure 2.10 and Figure 2.11 presents 1:1 plots of moist unit weight, dry unit weight, and moisture content for all the data obtained in this test study. It should be noted that the NDG data in Figure 2.10 and Figure 2.11 is from the direct transmission (DT) mode only.
Figure 2.10 1:1 Plots – Moist Unit Weight and Moisture Content
a) Moist Unit Weight: SC vs. NDG (DT)
b) Moist Unit Weight: Rubber Balloon vs. NDG (DT)
c) Moist Unit Weight: Box vs. NDG (DT)
d) Moisture Content: Oven Dried vs. NDG (DT)
Figure 2.11  1:1 Plots – Dry Unit Weight

a) Dry Unit Weight: SC vs. NDG (DT)

b) Dry Unit Weight: Rubber Balloon vs. NDG (DT)

c) Dry Unit Weight: Box vs. NDG (DT)
Results from this test study indicated that in situ densities determined by the direct transmission (DT) nuclear method using the factory calibration curve were as accurate as the densities obtained by the sand cone and rubber balloon methods. The direct transmission nuclear method, utilizing a calibration curve developed by WES, obtained density results that were slightly more accurate than the sand cone or rubber balloon method. It should also be noted that densities determined by the surface backscatter method were not very accurate when compared to conventional methods. Water contents using the factory calibration curve were not considered accurate enough for field use (68% of nuclear water contents were within ±3.81% of oven dried water contents, and 95% were within ±7.62%). Water contents using a calibration curve developed by WES were determined to be accurate enough for field use (68% of nuclear water contents were within ±1.23% of oven dried water contents, and 95% were within ±2.46%).

2.2.5 Variability in Field Density Tests (Noorany et al. 2000)

Noorany et al. (2000) performed a comparative study of the three most commonly used field density tests: sand cone, nuclear, and drive cylinder. A large hydraulic soil compaction apparatus was constructed for this test study to compact the soil in 4 inch lifts in a 4 foot mold with an inside diameter of 46 inches. A cohesive soil with gravel up to ¾ inch that classified as a clayey sand (SC) was used for this test study. Sand cone, nuclear, and drive cylinder tests were performed in all five series of tests executed in this study. The major conclusions Noorany and his colleagues determined from this test study were the following:
1) The sand cone method was the most accurate of all of the in-situ density tests, with measured relative compaction values that were a maximum of 5% off the placement values.

2) The nuclear density gauge test had a significantly wider range of variability than any of the other tests, with measured relative compaction values that were a maximum of 10% off the placement values. It should be noted that a significant source of error in the nuclear method measurements are from the moisture content readings, which varied significantly from direct measurement of water content by the oven dried method.

3) This study pointed out that the standard procedure for calibrating the nuclear device with a density block does not guarantee accurate density and water content prediction, and that it is necessary to calibrate the nuclear device for every type of soil at every site against direct measurements made with the sand cone or a similar method. It should be noted that when the nuclear density data was adjusted based on water contents directly measured by oven drying, results were more accurate and had less variability.

4) The drive cylinder method generally underestimated the field density and relative compaction, with measured relative compaction values that were a maximum of 8% lower than the placement value. The main reason for measuring low densities in this test study was due to the presence of gravel in the soil. Gravel created voids along the side wall of the drive cylinder, thus producing lower densities when gravel had to be removed from the sample ends during the trimming process.
Chapter 3

ELECTRICAL DENSITY GAUGE OPERATING PRINCIPLES

3.1 Electrical Density Gauge

The Electrical Density Gauge (EDG) is a new product on the market that can be used for compaction control of soil on construction projects. The EDG is a lightweight and portable battery powered device that is not subject to calibration degradation over time, regulatory control, or any safety precautions. ASTM D 7698, Standard Test Method for In-Place Estimation of Density and Water Content of Soil and Aggregate by Correlation with Complex Impedance was approved in March of 2011 and should be referenced when using and operating the EDG.

3.2 Operating Principles

The EDG contains a 3 MHz radio frequency source within the measurement circuit of the device. A radio frequency source is applied to the soil being tested through steel conical electrical probes that are pushed into the soil to a specific depth. A rubber hammer is used to push the 4 electrical probes into the ground in a square-shaped pattern using a plastic template, and alligator clips are then placed on each pair of electrical probes that are opposite from one another. The alligator clips are connected to an electrical soil measurement sensor that relays
information to the onboard computer in the device. The EDG has a temperature probe that records the temperature of the soil as well. Electrical measurements of AC current, voltage, and phase are made between the electrical probes. Readings are taken in a cross pattern at the test location in N-S, S-N, E-W, and W-E directions, and the average values of current, voltage, and phase are then used to determine the equivalent values of soil capacitance, resistance, and impedance. Figure 3.1 displays a typical setup of the EDG.

Figure 3.1  Typical EDG setup
The electrical dielectric parameters of the soil are calculated using standard electrical engineering equations that use current (I), voltage (V), and phase (θ) to determine the equivalent values of soil resistance (R) and soil capacitance (C). Once the soil resistance and soil capacitance are determined the complex impedance (Z) of the soil can be determined as well. It should be noted that a proprietary temperature compensation algorithm corrects the electrical values due to the effects of temperature if the temperature probe is used and the temperature correction mode is turned on.

From the electrical values measured and calculated by the EDG, correlations to physical soil properties obtained from the nuclear density gauge (NDG), sand cone, or other in-situ density and moisture content tests are made in order to develop a Soil Model. The following section will discuss how to create a Soil Model and the correlation relationships that are used to determine dry unit weight, moist unit weight, and moisture content at a given test location.

### 3.3 Field Calibration and Soil Model Development

A calibration Soil Model must be created before using the EDG for compaction control on a construction project. A Soil Model is the result of the calibration procedure that establishes a correlating linear function between measured electrical soil properties and measured physical soil properties. In order to create a Soil Model, the manufacturer recommends obtaining 6 field test points at three different moisture contents and two levels of compaction. For example, a user may want to try to obtain the following points to create a Soil Model:
1) 98% compaction at 5% moisture content
2) 98% compaction at 7.5% moisture content
3) 98% compaction at 10% moisture content
4) 92% compaction at 5% moisture content
5) 92% compaction at 7.5% moisture content
6) 92% compaction at 10% moisture content

After each EDG test is conducted at a specific test location, a NDG, sand cone, or other in-situ density test must be conducted at the same test location. The physical soil properties obtained from the NDG, sand cone, or other in situ test are then used to correlate to the electrical properties previously measured at the same test location. Once the physical soil properties are obtained from the NDG, sand cone, or other type of test they can be entered into the EDG. After all physical tests are completed and entered into the EDG, Soil Model calibration curves are developed and can be viewed on the device. The following linear calibration relationships are used to determine physical soil properties, where $\gamma_m$ is the moist unit weight of soil obtained from a physical test, $Z$ is the complex impedance determined from the EDG electrical measurements, $m_1$ is the slope of the linear equation obtained from correlating $\gamma_m$ and $Z$, $b_1$ is the intercept of the linear equation obtained from correlating $\gamma_m$ and $Z$, $W_w$ is the weight of water per unit volume obtained from a physical test, $(C/R)$ is the ratio of soil capacitance over soil resistance determined from the EDG electrical measurements, $m_2$ is the slope of the linear equation obtained from correlating $W_w$ and $(C/R)$, and $b_2$ is the intercept obtained from correlating $W_w$ and $(C/R)$:
\[ \gamma_m = m_1 \times Z + b_1 \quad (3.1) \]
\[ W_w = m_2 \times (C/R) + b_2 \quad (3.2) \]

It should be noted that there is an option to apply a proprietary temperature correction algorithm to the recorded values of \( Z \) and \( C/R \), to account for the effect of temperature on the measured results. Once all calibration tests are completed and a soil model is created, the EDG is ready to be used on a field site. A new Job Site is created on the EDG, and the soil model previously developed is then assigned to the new job site (See EDG Product manual for instructions).

When an EDG test is performed in the field, the electrical properties of the specific test location are measured by the EDG and are used as input for the calibration equations that have been previously developed. The measured complex impedance (\( Z \)) and ratio of soil capacitance over soil resistance (\( C/R \)) for the given test location are plugged into the calibration equations, and the corresponding moist unit weight and weight of water per unit volume are calculated. The following standard geotechnical engineering equations are then used to determine dry unit weight and moisture content of the soil, where \( \gamma_d \) is dry unit weight and \( w \) is moisture content:

\[ \gamma_m - W_w = \gamma_d \quad (3.3) \]
\[ w = \frac{\gamma_m}{\gamma_d} - 1 \quad (3.4) \]

It should be noted that the relative compaction (in %) can also be measured by the EDG if a standard effort or modified effort compaction test (ASTM D
698 or ASTM D 1557) has been run on the soil that is being tested in the field. The maximum dry unit weight of the soil determined from the compaction test is entered into the EDG, and the percent compaction is calculated using the following equation, where \( RC(\%) \) is the relative percent compaction, \( \gamma_{d\text{-measured}} \) is the value of dry unit weight that is determined by the EDG at a given in situ location, and \( \gamma_{d\text{-max}} \) is the maximum dry unit weight determined from the compaction test:

\[
RC(\%) = \frac{\gamma_{d\text{-measured}}}{\gamma_{d\text{-max}}} \tag{3.5}
\]

After an EDG test has been performed, the computer monitor on the EDG displays the moist unit weight, dry unit weight, weight of water per unit volume, moisture content, and percent compaction of the test location immediately after the electrical measurements are taken.
4.1 Introduction

In July 2009, experimental field studies were performed on 2 different active construction projects in the state of Delaware to investigate the feasibility for the Delaware Department of Transportation (DELDOT) to adopt a new in-situ field compaction control device, the Electrical Density Gauge (EDG). One of these projects was located in Dover, DE, and the other was located in Middletown, DE; hereafter, for purposes of confidentiality, these projects will be generically referred to as the “Dover” and “Middletown” projects. For both of these active construction projects, DELDOT technicians aided in the execution of multiple small scale field studies.

4.2 Soil Properties

4.2.1 Soil Properties for Fill Materials Used on the Dover Project

The soil used as fill material at the construction site in Dover was taken from a borrow pit area across from the new overpass being constructed near Route 1 and the DELDOT main office. Soil samples at the Dover project site were generally a light gray to light brown silty clayey sand with trace amounts of fine gravel (ASTM D 2488). Figure 4.1 and Figure 4.2 are photos from the construction site in Dover. During the in situ testing process with the EDG, the soils that were placed at each in situ test location were observed to be somewhat variable in nature. This observation
was reinforced by visits to the soil borrow area, where distinct layers of silty sand and clayey silts were observed in the borrow pit (ASTM D 2488).

![Figure 4.1 Dover Construction Site](image)

Figure 4.1   Dover Construction Site

![Figure 4.2 An EDG test location at the Dover Site](image)

Figure 4.2   An EDG test location at the Dover Site
In an attempt to quantify the soil variability that was observed, sieve analysis tests were conducted in general accordance with ASTM D 6913 on 8 samples that were taken from a few of the in situ test locations at the Dover site (Figure 4.3). Table 4.1 provides overall gradation information for the soil, as determined from the 8 samples that were analyzed from the field site.

Table 4.1  General Summary Table of Classification Results – DOVER

<table>
<thead>
<tr>
<th></th>
<th>MIN</th>
<th>MAX</th>
<th>MEAN</th>
<th>STD</th>
<th>CV (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. 4 (%)</td>
<td>94.14</td>
<td>98.91</td>
<td>96.40</td>
<td>1.56</td>
<td>1.62%</td>
</tr>
<tr>
<td>No. 10 (%)</td>
<td>90.95</td>
<td>97.22</td>
<td>93.77</td>
<td>2.12</td>
<td>2.26%</td>
</tr>
<tr>
<td>No. 40 (%)</td>
<td>53.09</td>
<td>71.20</td>
<td>62.01</td>
<td>6.09</td>
<td>9.83%</td>
</tr>
<tr>
<td>No. 200 (%)</td>
<td>23.73</td>
<td>39.45</td>
<td>31.26</td>
<td>5.83</td>
<td>18.64%</td>
</tr>
<tr>
<td>% gravel</td>
<td>1.09</td>
<td>5.86</td>
<td>3.60</td>
<td>1.56</td>
<td>43.29%</td>
</tr>
<tr>
<td>% sand</td>
<td>57.03</td>
<td>70.41</td>
<td>65.14</td>
<td>5.47</td>
<td>8.40%</td>
</tr>
<tr>
<td>% fines</td>
<td>23.73</td>
<td>39.45</td>
<td>31.26</td>
<td>5.83</td>
<td>18.64%</td>
</tr>
</tbody>
</table>
4.2.2 Soil Properties for Fill Materials Used on the Middletown Project

The soil tested at the construction site in Middletown was from a borrow pit within a half mile of the site. Soil samples at the Middletown project site were generally a brown silty sand with trace amounts of fine gravel (ASTM D 2488). Figure 4.4 and Figure 4.5 are photos from the construction site in Middletown.
Sieve analysis tests were conducted in general accordance with ASTM D 6913 on 8 samples that were taken from a few in situ test locations at the Middletown site (Figure 4.6). A few Atterberg limit tests (ASTM D 4318) conducted
on the finer portion of the soils indicated that the soils examined in this study had fines that were nonplastic (NP) in nature. The soil samples consequently are classified as either silty sand (SM), or poorly-graded sand with silt (SP-SM) according to the Unified Soil Classification System (ASTM D 2487). Table 4.2 provides overall gradation information for the soil, as determined from the 8 samples that were analyzed from the field site. It should be noted that the coefficients of variation of the soil tested at the Middletown site are lower than the coefficient of variations for the soil tested from the Dover site.

<table>
<thead>
<tr>
<th></th>
<th>MIN</th>
<th>MAX</th>
<th>MEAN</th>
<th>STD</th>
<th>CV (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. 4 (%)</td>
<td>96.53</td>
<td>98.76</td>
<td>97.96</td>
<td>0.68</td>
<td>0.70%</td>
</tr>
<tr>
<td>No. 10 (%)</td>
<td>95.05</td>
<td>97.92</td>
<td>96.64</td>
<td>0.90</td>
<td>0.93%</td>
</tr>
<tr>
<td>No. 40 (%)</td>
<td>52.54</td>
<td>63.65</td>
<td>58.10</td>
<td>4.17</td>
<td>7.19%</td>
</tr>
<tr>
<td>No. 200 (%)</td>
<td>10.51</td>
<td>17.83</td>
<td>14.82</td>
<td>2.22</td>
<td>15.01%</td>
</tr>
<tr>
<td>% gravel</td>
<td>1.24</td>
<td>3.47</td>
<td>2.04</td>
<td>0.68</td>
<td>33.53%</td>
</tr>
<tr>
<td>% sand</td>
<td>80.81</td>
<td>87.44</td>
<td>83.14</td>
<td>2.13</td>
<td>2.56%</td>
</tr>
<tr>
<td>% fines</td>
<td>10.51</td>
<td>17.83</td>
<td>14.82</td>
<td>2.22</td>
<td>15.01%</td>
</tr>
</tbody>
</table>
4.3 In-Situ Field Testing Procedure

On both active construction projects, Nuclear Density Gauge (NDG) and EDG tests were performed at the same approximate in situ locations on previously compacted areas of roadway subgrade. Three one-minute NDG readings and 1 EDG test were taken at each in situ test location. The average of the three one-minute NDG readings was used as a calibration input value for developing the appropriate EDG soil model for the fill materials used in each field project (See Chapter 3 for EDG soil model concepts). In addition, for both field projects, bag samples were taken at each in situ test location for later soil classification testing.
Following the approach presented in Chapter 3 (the manufacturer recommended approach for building soil models), EDG soil model calibration curves were developed for each specific testing site (DOVER and MDLTOWN) using the measured NDG test results for soil model calibration. The calibration curves developed for each individual soil model were then used to predict the in-situ soil property values for each test location.

As discussed in Chapter 3, temperature can sometimes have a significant effect on measured EDG test results. In order to investigate the effect of the temperature correction that is used on the EDG calibration relationships, soil models were developed with and without using the proprietary EDG temperature correction algorithm.

### 4.4 Results: In-Situ Field Testing

The in-situ field tests described in this section were conducted to create a series of soil models using the field calibration method that is recommended by the manufacturer of the electrical density gauge (EDG, LLC). From the measured NDG and EDG values, it is possible to build a series of series of calibration curves, and then use these curves to convert the measured raw electrical values to predictions of soil unit weight and soil moisture content. Following this approach, it is possible to perform comparisons between the measured NDG in-situ test values and the predicted EDG test values for each soil type.

Direct comparison of the EDG-predicted values with the measured NDG values provides a useful tool for assessing the effect of soil model calibration scatter on the actual engineering properties that result (e.g., unit weight, moisture content). However, this assessment procedure is inherently unreliable for assessing the ability of...
the EDG to make accurate predictions of soil moisture content and soil density (or unit weight). This is because the calibration data set is the same as the assessment data set, and consequently the results do not represent a truly “blind” assessment of the EDG’s ability to measure the in situ soil properties of interest. A truly blind assessment of the type that is recommended is provided in Chapter 6, for a separate series of “box” assessment tests. However, as independent measurements of soil density and moisture content outside of the calibration data set were not performed during the field studies described in this section, the only option here was to use the same data set for forward prediction as what was used for soil model calibration.

Calibration curves for each of the soil models that were created are presented in the following sections. Also, 1:1 plots that compare NDG measured values versus EDG predicted values are presented, along with relative error histogram plots between the measured and predicted values. The in-situ measured soil properties assessed in this study were: moist unit weight ($\gamma_{mu}$), weight of water per unit volume ($W_W$), dry unit weight ($\gamma_{du}$), and moisture content ($w$).

### 4.4.1 Calibration Curves

### 4.4.2 Dover Calibration

At the Dover project site, the fill material from the borrow source was observed to be somewhat variable, as noted previously. The associated calibration curves for the soil model are presented in Figure 4.7. The coefficient of determination ($R^2$) values are presented on each graph in Figure 4.7 as well. It should be noted that the soil model calibration curves in Figure 4.7a and Figure 4.7c for the DOVER Soil Model (TC OFF & TC ON), show an increase in $R^2$ from 0.0259 to 0.3639 when the
EDG temperature correction algorithm is applied. For the DOVER Soil Model, the $R^2$ values for the calibration curves with the EDG temperature correction algorithm applied are greater than the $R^2$ values for the calibration curves with no EDG temperature correction algorithm applied. Table 4.3 provides a summary of the $R^2$ values, slopes, and intercepts of the calibration curves for the DOVER Soil Model (TC OFF & TC ON).

4.4.3 Middletown Calibration

The EDG soil model created in this study was carried out at multiple locations throughout the Middletown construction site. The in-situ field tests were performed on different sections of previously compacted roadway subgrade.

The associated calibration curves for the soil model are presented in Figure 4.7. The coefficient of determination ($R^2$) values are presented on each graph in Figure 4.7 as well. For the MDLTOWN Soil Model, the $R^2$ values for the calibration curves with the EDG temperature correction algorithm applied are basically the same as the $R^2$ values for the calibration curves with no EDG temperature correction algorithm applied. Table 4.4 provides a summary of the $R^2$ values, slopes, and intercepts of the calibration curves for the MDLTOWN Soil Model (TC OFF & TC ON).
**Figure 4.7** Calibration Curves  

- **a)** DOVER Soil Model: $\gamma_{m\text{-NDG}}$ vs. $Z$  
- **b)** DOVER Soil Model: $W_{w\text{-NDG}}$ vs. C/R  
- **c)** MDLTOWN Soil Model: $\gamma_{m\text{-NDG}}$ vs. $Z$  
- **d)** MDLTOWN Soil Model: $W_{w\text{-NDG}}$ vs. C/R
Table 4.3  General Summary Table of Calibration Curves – DOVER Soil Model

<table>
<thead>
<tr>
<th>DOVER Soil Model</th>
<th>Calibration Curve</th>
<th>( R^2 )</th>
<th>Slope</th>
<th>Intercept</th>
</tr>
</thead>
<tbody>
<tr>
<td>TC OFF</td>
<td>( \gamma_m ) vs. Z</td>
<td>0.0259</td>
<td>-0.0022</td>
<td>20.4399</td>
</tr>
<tr>
<td>TC ON</td>
<td>( \gamma_m ) vs. Z</td>
<td>0.3639</td>
<td>-0.0047</td>
<td>22.8434</td>
</tr>
<tr>
<td>TC OFF</td>
<td>( W_w ) vs. C/R</td>
<td>0.2451</td>
<td>8.1983</td>
<td>0.7578</td>
</tr>
<tr>
<td>TC ON</td>
<td>( W_w ) vs. C/R</td>
<td>0.3415</td>
<td>11.4662</td>
<td>0.7194</td>
</tr>
</tbody>
</table>

Table 4.4  General Summary Table of Calibration Curves – MDLTOWN Soil Model

<table>
<thead>
<tr>
<th>MDLTOWN Soil Model</th>
<th>Calibration Curve</th>
<th>( R^2 )</th>
<th>Slope</th>
<th>Intercept</th>
</tr>
</thead>
<tbody>
<tr>
<td>TC OFF</td>
<td>( \gamma_m ) vs. Z</td>
<td>0.1457</td>
<td>-0.0010</td>
<td>20.0519</td>
</tr>
<tr>
<td>TC ON</td>
<td>( \gamma_m ) vs. Z</td>
<td>0.1199</td>
<td>-0.0007</td>
<td>22.0568</td>
</tr>
<tr>
<td>TC OFF</td>
<td>( W_w ) vs. C/R</td>
<td>0.9099</td>
<td>5.3701</td>
<td>0.9092</td>
</tr>
<tr>
<td>TC ON</td>
<td>( W_w ) vs. C/R</td>
<td>0.8832</td>
<td>6.0238</td>
<td>0.9688</td>
</tr>
</tbody>
</table>

4.5 1:1 Plots

The following sections show 1:1 plots that compare NDG measured values versus EDG predicted values. An explanation of statistical variables used to interpret the 1:1 plots is given below prior to explanation of the 1:1 plots.
4.5.1 Statistical Measures

The root-mean-square error (RMSE) is a frequently used measure of the differences between values predicted by a model and the values actually observed from the variable being estimated, and is a good measure of precision. RMSE is calculated by taking the square root of the mean square error; for an unbiased estimator, the RMSE is the square root of the variance (Freedman 1998) (Equation 4.1):

\[
RMSE = \sqrt{\frac{\sum_{i=1}^{n} (\hat{y}_{i,j} - y_{2,i})^2}{n}}
\]  

(4.1)

The coefficient of variation of the RMSE (CV(RMSE)), is defined as the RMSE normalized to the mean of the observed values (Freedman 1998). It is the same concept as the coefficient of variation except that RMSE replaces the standard deviation.

\[
CV(RMSE) = \frac{RMSE}{\bar{x}}
\]  

(4.2)

The normalized root-mean-square error (NRMSE) is the RMSE divided by the range of observed values and is often expressed as a percentage, where lower values indicate less residual variance (Freedman 1998).

\[
NRMSE = \frac{RMSE}{x_{\text{max}} - x_{\text{min}}}
\]  

(4.3)

4.5.2 1:1 Plots – DOVER Soil

The DOVER Soil Model calibration curves were used to predict the EDG values that are presented in this section. Figure 4.8a shows NDG measured moist unit weights (γ_{m-NDG}) versus EDG predicted moist unit weights (γ_{m-EDG}) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 4.8b
shows NDG measured dry unit weights ($\gamma_{d,NDG}$) versus EDG predicted dry unit weights ($\gamma_{d,EDG}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 4.8c shows NDG measured weight of water per unit volume ($W_{w,NDG}$) versus EDG predicted weight of water per unit volume ($W_{w,EDG}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 4.8d shows NDG measured moisture contents ($w_{NDG}$) versus EDG predicted moisture contents ($w_{EDG}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). It should be noted that the solid line in Figure 4.8a, 4.8b, 4.8c, and 4.8d is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$ in Figure 4.8a, 4.8b, and 4.8c, and ±0.5 % lines in Figure 4.8d, which are provided for reference.

For the DOVER Soil, the RMSE, CV(RMSE), and NRMSE values for moist unit weight, dry unit weight, weight of water per unit volume, and moisture content are all slightly greater with no EDG temperature correction algorithm applied. Table 4.5 summarizes the statistical values for the DOVER Soil.

| Table 4.5 | Summary of Statistical Measures – DOVER Soil |

<table>
<thead>
<tr>
<th></th>
<th>DOVER Soil (TC OFF)</th>
<th>DOVER Soil (TC ON)</th>
</tr>
</thead>
<tbody>
<tr>
<td>RMSE</td>
<td>0.547</td>
<td>0.443</td>
</tr>
<tr>
<td>CV(RMSE)</td>
<td>0.028</td>
<td>0.023</td>
</tr>
<tr>
<td>NRMSE</td>
<td>0.290</td>
<td>0.235</td>
</tr>
</tbody>
</table>
Figure 4.8  1:1 Plots – DOVER Soil  
  a) 1:1 Plot – Moist Unit Weight  
  b) 1:1 Plot – Dry Unit Weight  
  c) 1:1 Plot – Wt. of Water per Unit Volume  
  d) 1:1 Plot – Moisture Content
4.5.3 1:1 Plots – MDLTOWN Soil

The MDLTOWN Soil Model calibration curves were used to predict the EDG values that are presented in this section. Figure 4.9a shows NDG measured moist unit weights ($\gamma_{m-\text{NDG}}$) versus EDG predicted moist unit weights ($\gamma_{m-\text{EDG}}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 4.9b shows NDG measured dry unit weights ($\gamma_{d-\text{NDG}}$) versus EDG predicted dry unit weights ($\gamma_{d-\text{EDG}}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 4.9c shows NDG measured weight of water per unit volume ($W_{W-\text{NDG}}$) versus EDG predicted weight of water per unit volume ($W_{W-\text{EDG}}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 4.9d shows NDG measured moisture contents ($w_{\text{NDG}}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). It should be noted that the solid line in Figure 4.9a, 4.9b, 4.9c, and 4.9d is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$ in Figure 4.9a, 4.9b, and 4.9c, and ±0.5 % lines in Figure 4.9d for reference.

For the MDLTOWN Soil, the RMSE, CV(RMSE), and NRMSE values for moist unit weight, weight of water per unit volume, and moisture content are all slightly greater with the EDG temperature correction algorithm applied. For SM MDLTOWN, the RMSE, CV(RMSE), and NRMSE values for dry unit weight are slightly greater with no EDG temperature correction algorithm applied. Table 4.6 summarizes the statistical values for the MDLTOWN Soil.
Figure 4.9 1:1 Plots - MDLTOWN Soil
a) 1:1 Plot – Moist Unit Weight
b) 1:1 Plot – Dry Unit Weight
c) 1:1 Plot – Wt. of Water per Unit Volume
d) 1:1 Plot – Moisture Content
### Table 4.6  Summary of Statistical Measures –MDLTOWN Soil

<table>
<thead>
<tr>
<th>MDLTOWN Soil</th>
<th>(TC OFF)</th>
<th>(TC ON)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\gamma_m$</td>
<td>$W_w$</td>
</tr>
<tr>
<td>RMSE</td>
<td>0.341</td>
<td>0.117</td>
</tr>
<tr>
<td>CV(RMSE)</td>
<td>0.017</td>
<td>0.070</td>
</tr>
<tr>
<td>NRMSE</td>
<td>0.244</td>
<td>0.103</td>
</tr>
</tbody>
</table>

### 4.6 Relative Error

Relative error is calculated by taking the value considered to be the “actual” value, subtracting it from the “predicted” value, and dividing the resulting difference by the “actual” value. (Freedman 1998) (Equation 4.4):

$$\text{Relative error (\%)} = \frac{\text{NDG}_\text{VALUE} - \text{EDG}_\text{VALUE}}{\text{NDG}_\text{VALUE}} \times 100 \quad (4.4)$$

The following section shows histograms of the relative error calculated for moist unit weight, weight of water per unit volume, dry unit weight, and moisture content for the DOVER and MDLTOWN soils. A cumulative distribution function (CDF) is displayed on each histogram as well.

#### 4.6.1 Relative Error: DOVER Soil

Figure 4.10a is a histogram plot of relative error between $\gamma_m$-NDG and $\gamma_m$-EDG (TC ON & TC OFF). For the DOVER Soil (TC OFF), relative error values for $\gamma_m$ range from -5.43% to 4.10%, and for the DOVER Soil (TC ON) relative error values for $\gamma_m$ range from -4.42% to 4.02%.

Figure 4.10b is a histogram plot of relative error between $\gamma_d$-NDG and $\gamma_d$-EDG (TC ON & TC OFF). For the DOVER Soil (TC OFF), relative error values for $\gamma_d$
range from -5.48% to 4.62%, and for the DOVER Soil (TC ON) relative error values for $\gamma_d$ range from -4.63% to 3.90%.

Figure 4.10c is a histogram plot of relative error between $W_{W\text{-}NDG}$ and $W_{W\text{-}EDG}$ (TC ON & TC OFF). For the DOVER Soil (TC OFF), relative error values for $W_w$ range from -32.78% to 30.76%, and for the DOVER Soil (TC ON) relative error values for $W_w$ range from -25.80% to 29.35%.

Figure 4.10d is a histogram plot of relative error between $w_{NDG}$ and $w_{EDG}$ (TC ON & TC OFF). For the DOVER Soil (TC OFF), relative percent error values for $w$ range from -34.10% to 30.81%, and for the DOVER Soil (TC ON), relative percent error values for $w$ range from -25.92% to 30.13%.

Table 4.7 provides a summary of the minimum, maximum, range, and mean of the relative error histograms for the DOVER Soil (TC ON & TC OFF).

Table 4.7 Summary Table of Relative Error (%) – DOVER Soil

<table>
<thead>
<tr>
<th></th>
<th>(TC OFF)</th>
<th>(TC ON)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\gamma_m$</td>
<td>$W_w$</td>
</tr>
<tr>
<td>MIN</td>
<td>-5.43</td>
<td>-32.78</td>
</tr>
<tr>
<td>MAX</td>
<td>4.10</td>
<td>30.76</td>
</tr>
<tr>
<td>RANGE</td>
<td>9.53</td>
<td>63.54</td>
</tr>
<tr>
<td>MEAN</td>
<td>-0.08</td>
<td>-3.24</td>
</tr>
</tbody>
</table>

### 4.6.2 Relative Error: SM MDLTOWN

Figure 4.11a is a histogram plot of relative error between $\gamma_{m\text{-}NDG}$ and $\gamma_{m\text{-}EDG}$ (TC ON & TC OFF). For the MDLTOWN Soil (TC OFF), relative error values
for $\gamma_m$ range from -4.14% to 3.27%, and for the MDLTOWN Soil (TC ON) relative error values for $\gamma_m$ range from -4.23% to 3.21%.

Figure 4.11b is a histogram plot of relative error between $\gamma_d$-NDG and $\gamma_d$-EDG (TC ON & TC OFF). For the MDLTOWN Soil (TC OFF), relative error values for $\gamma_d$ range from -4.02% to 3.48%, and for the MDLTOWN Soil (TC ON) relative error values for $\gamma_d$ range from -4.20% to 3.47%.

Figure 4.11c is a histogram plot of relative error between $W_W$-NDG and $W_W$-EDG (TC ON & TC OFF). For the MDLTOWN Soil (TC OFF), relative error values for $W_W$ range from -16.48% to 12.96%, and for the MDLTOWN Soil (TC ON) relative error values for $W_W$ range from -18.02% to 15.79%.

Figure 4.11d is a histogram plot of relative error between $w_{NDG}$ and $w_{EDG}$ (TC ON & TC OFF). For the MDLTOWN Soil (TC OFF), relative error values for $w$ range from -16.57% to 13.37%, and for the MDLTOWN Soil (TC ON), relative error values for $w$ range from -15.18% to 16.16%.

Table 4.8 provides a summary of the minimum, maximum, range, and mean of the relative error histograms for the MDLTOWN Soil (TC ON & TC OFF).

<table>
<thead>
<tr>
<th>Table 4.8</th>
<th>Summary Table of Relative Error (%) – MDLTOWN Soil</th>
</tr>
</thead>
<tbody>
<tr>
<td>MDLTOWN Soil (TC OFF)</td>
<td>(TC ON)</td>
</tr>
<tr>
<td>$\gamma_m$</td>
<td>$W_w$</td>
</tr>
<tr>
<td>MIN</td>
<td>-4.14</td>
</tr>
<tr>
<td>MAX</td>
<td>3.27</td>
</tr>
<tr>
<td>RANGE</td>
<td>7.41</td>
</tr>
<tr>
<td>MEAN</td>
<td>-0.03</td>
</tr>
</tbody>
</table>
Figure 4.10  Relative Error Histograms and CDF Plots – DOVER Soil
a) Histogram & CDF – Moist Unit Weight (TC OFF & TC ON)
b) Histogram & CDF – Dry Unit Weight (TC OFF & TC ON)
c) Histogram & CDF – Wt. of Water per Unit Volume (TC OFF & TC ON)
d) Histogram & CDF - Moisture Content (TC OFF & TC ON)
Figure 4.11  Relative Error Histograms and CDF Plots – MDLTOWN Soil
  a) Histogram & CDF – Moist Unit Weight (TC OFF & TC ON)
  b) Histogram & CDF – Dry Unit Weight (TC OFF & TC ON)
  c) Histogram & CDF – Wt. of Water per Unit Volume (TC OFF & TC ON)
  d) Histogram & CDF - Moisture Content (TC OFF & TC ON)
4.7 Summary of Results

4.7.1 Summary of DOVER Soil Results

The soil model created using the field calibration procedure at the Dover construction site had particularly low $R^2$ values for the calibration curves. The $R^2$ values for the temperature compensated calibration curves for all soil models were slightly higher in all cases (Table 4.1). Generally, the RMSE, CV(RMSE), and NRMSE values were greater when no EDG temperature correction algorithm was applied. Differences in relative error between the NDG and EDG predicted values for the calibration curves with and without the EDG temperature correction algorithm applied are generally minimal. In addition, the standard deviation from the average for each set of EDG predicted values (TC ON & TC OFF) is lower than the standard deviation from the average for the corresponding NDG measured values; this observation manifests itself as a smoothing effect, which can be observed on the moist unit weight and dry unit weight 1:1 plots for the DOVER Soil (Figure 4.8a, 4.8c). Table 4.9 provides a summary of the standard deviation values for the DOVER Soil.
Table 4.9  Summary Table of Standard Deviation values for the DOVER Soil

<table>
<thead>
<tr>
<th></th>
<th>DOVER Soil: Standard Deviation, σd</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>γm</td>
</tr>
<tr>
<td>NDG</td>
<td>0.57</td>
</tr>
<tr>
<td>EDG (TC OFF)</td>
<td>0.09</td>
</tr>
<tr>
<td>EDG (TC ON)</td>
<td>0.34</td>
</tr>
</tbody>
</table>

4.7.2  Summary of MDLTOWN Soil Results

The soil models created using the field calibration procedure at the Middletown construction site had higher R² values for the calibration curves than the Dover site. The R² values for the temperature compensated calibration curves for all soil models were basically the same as the R² values for the calibration curves with no temperature correction (Table 4.4). Generally, the RMSE, CV(RMSE), and NRMSE values were greater when the EDG temperature correction algorithm was applied. Differences in relative error between the NDG and EDG predicted values for the calibration curves with and without the EDG temperature correction algorithm applied are generally minimal. In addition, the standard deviation from the average for each set of EDG predicted density values (only dry unit weight and moist unit weight) is generally lower than the standard deviation from the average for the corresponding NDG measured values; this observation manifests itself as a smoothing effect, which can be observed on the moist unit weight and dry unit weight 1:1 plots for the MDLTOWN Soil (Figure 4.9a, 4.9c). Table 4.10 provides a summary of the standard deviation values for the MDLTOWN Soil.
Table 4.10  Summary Table of Standard Deviation values for the MDLTOWN Soil

<table>
<thead>
<tr>
<th></th>
<th>$\gamma_m$</th>
<th>$W_w$</th>
<th>$\gamma_d$</th>
<th>$w$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NDG</td>
<td>0.38</td>
<td>0.38</td>
<td>0.39</td>
<td>2.21</td>
</tr>
<tr>
<td>EDG (TC OFF)</td>
<td>0.14</td>
<td>0.38</td>
<td>0.25</td>
<td>2.27</td>
</tr>
<tr>
<td>EDG (TC ON)</td>
<td>0.13</td>
<td>0.35</td>
<td>0.23</td>
<td>2.07</td>
</tr>
</tbody>
</table>

4.8 Discussion of Results and Conclusions

From the raw data and associated analysis that is presented in this chapter, it is clear that there are some limitations to creating a soil model using the field calibration process. In particular, for the data that was recorded during these two field studies, relatively poor agreement was observed between the NDG and EDG predicted values. This lack of agreement occurred even when the “assessment” data set was the same as the “calibration” data set, which is a much less rigorous test than a truly “blind” assessment (as discussed previously).

There are a number of possible causes for the general lack of agreement that was observed. Some of the more notable reasons that are believed to have been possible contributing factors in this field study include:

- Difficulties in constructing a soil model that is representative of the range of moisture contents and soil densities that will be encountered during the compaction process. In particular, on an active construction site, contractors try to maintain the same moisture content and reach the same density for the fill material they are compacting. This creates difficulty when trying to build a soil model that spans the range of densities and moisture contents that may be
encountered in a fair and representative way. Getting the necessary field variability in moisture content can be particularly challenging under certain field conditions.

- Inherent uncertainties and sources of error in the tests that are used for the field calibration purposes themselves. In particular, the field calibration process requires the use of a NDG or other standard in-situ density test like the sand cone or rubber balloon test. These tests have their own uncertainty and sources of error in measurement, and consequently this error has the potential to become compounded when building a soil model.

- Soil variability on site. The EDG appears to be more sensitive than the NDG to variations in the soil borrow source. This effect is evident if the results from the Dover project are compared against those from the Middletown project. In particular, changes in the quantity or nature of the fines in a borrow soil are believed to have a significant effect on measured EDG results. This is because the electrical characteristics of a soil matrix are significantly affected by the characteristics of the finer particles in the matrix.

- Another observation captured by the preliminary field studies discussed in this chapter is that the EDG temperature correction algorithm can lower the $R^2$ values for the calibration curves, thus not improving the results. The EDG temperature correction algorithm does not seem to properly capture the effect of temperature on the soils that were tested in this field study. An assessment of the effectiveness of the EDG temperature correction algorithm will be the focus of future research.
After a considerable amount of time and effort trying to get the necessary data on active construction projects, it was determined that an alternative approach was needed to generate data that could be used to fairly assess the EDG. The wide range of moisture contents and densities needed to build proper calibration curves made obtaining a calibration soil model challenging on an active construction site, in part because of contractor demands, budget constraints, and compaction control requirements. Additionally, the somewhat non-uniform soil conditions at the Dover project yielded unusually poor calibration curves, and made deployment of the gauge on this project problematic.

The decision to stop utilizing a field calibration approach for the EDG also coincided with the development of a new type of “soil mold” laboratory calibration procedure that was developed by EDG, LLC, that could potentially be used to build superior soil models. This laboratory calibration procedure presents a desirable alternative to field calibration, and its implementation will be discussed in more detail in the following chapter (Chapter 5).
CHAPTER 5
MOLD CALIBRATION PROCEDURE & RESULTS

5.1 Introduction

During the progress of this research study, EDG, LLC. developed a new calibration procedure. This new calibration procedure still adheres to the same general principles of creating a soil model (See Chapter 3), but calibration test points are not gathered in the field and traditional in-situ compaction control tests (NDG, sand cone, etc.) are not used for correlation purposes. Instead, calibration test points are gathered by preparing soil at various moisture contents and densities using a large “Proctor”-type mold having an inside diameter of 378 mm (14.88 in.) and a depth of 254 mm (10 in.) (Figure 5.1).

Figure 5.1 Large “Proctor” type mold and tamper
5.2 **Soil Properties**

The soil used for the soil model mold calibration tests was from a borrow pit at the Greggo & Ferrara facilities in Delaware. A truckload of soil was donated by Greggo & Ferrara and dumped at the DELDOT facility in Bear, Delaware for usage during this research study. Visual-manual classification of soil samples from the borrow pit indicated that this soil was generally a brown silty sand with trace amounts of fine gravel (ASTM D 2488). Figure 5.2 is a photo of a portion of the stockpile that was used for testing, located at the DELDOT facility in Bear.

![Soil Stockpile at DELDOT facility in Bear, DE](image)

**Figure 5.2  Soil Stockpile at DELDOT facility in Bear, DE**

Sieve analysis and hydrometer tests were conducted in general accordance with ASTM D 6913 and ASTM D 422-63 on samples from all 12 of the mold tests that were conducted. From these tests, 10 of the soil samples classified as a silty sand
(SM) and 2 samples classified as poorly-graded sand with silt (SP-SM), according to the Unified Soil Classification System (ASTM D 2487). Table 5.1 provides overall gradation information for the soil, as determined from the 12 samples that were analyzed from the mold tests.

![Figure 5.3 Gradation distributions for soil samples from mold tests](image)

Figure 5.3  Gradation distributions for soil samples from mold tests
Table 5.1  General Summary Table of Classification Results – Mold Tests

<table>
<thead>
<tr>
<th></th>
<th>MIN</th>
<th>MAX</th>
<th>MEAN</th>
<th>STD</th>
<th>CV (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. 4 (%)</td>
<td>88.28</td>
<td>97.70</td>
<td>94.42</td>
<td>2.69</td>
<td>2.85%</td>
</tr>
<tr>
<td>No. 10 (%)</td>
<td>83.96</td>
<td>94.47</td>
<td>91.02</td>
<td>3.04</td>
<td>3.34%</td>
</tr>
<tr>
<td>No. 40 (%)</td>
<td>49.45</td>
<td>52.77</td>
<td>51.25</td>
<td>0.91</td>
<td>1.77%</td>
</tr>
<tr>
<td>No. 200 (%)</td>
<td>14.29</td>
<td>20.65</td>
<td>17.01</td>
<td>1.98</td>
<td>11.62%</td>
</tr>
<tr>
<td>% gravel</td>
<td>2.30</td>
<td>11.72</td>
<td>5.58</td>
<td>2.69</td>
<td>48.24%</td>
</tr>
<tr>
<td>% sand</td>
<td>70.05</td>
<td>85.94</td>
<td>80.09</td>
<td>4.64</td>
<td>5.80%</td>
</tr>
<tr>
<td>% fines</td>
<td>11.44</td>
<td>18.22</td>
<td>14.33</td>
<td>2.14</td>
<td>14.94%</td>
</tr>
<tr>
<td>% silt</td>
<td>6.60</td>
<td>9.50</td>
<td>7.89</td>
<td>0.95</td>
<td>12.01%</td>
</tr>
<tr>
<td>% clay</td>
<td>6.30</td>
<td>10.70</td>
<td>7.89</td>
<td>1.35</td>
<td>17.07%</td>
</tr>
<tr>
<td>Cu</td>
<td>48.54</td>
<td>337.84</td>
<td>172.20</td>
<td>110.73</td>
<td>64.30%</td>
</tr>
<tr>
<td>Cc</td>
<td>14.16</td>
<td>85.76</td>
<td>43.82</td>
<td>23.96</td>
<td>54.69%</td>
</tr>
</tbody>
</table>

5.3  Mold Calibration Procedure

The outer frame of the mold is constructed from a section of 378 mm (14.88 in.) inside-diameter and 389 mm (15.32 in.) outside-diameter polyvinyl chloride (PVC) pipe. The base of the mold is constructed of a highly durable plastic material. Plastics are used for the mold construction because they are insulators and will not interfere with the electrical measurements carried out by the EDG in the same fashion that a metal (conductive) mold might.

It should be noted that this calibration procedure is relatively new and innovative, and consequently it is not included in the ASTM approved methodology for the EDG (ASTM D 7698-11 – Standard Test Method for In-Place Estimation of Density and Water Content of Soil and Aggregate by Correlation with Complex Impedance).
The following procedure was utilized when performing mold calibration tests for this research study:

1) Prepare the soil at the desired moisture content and wait 24 hours for the moisture in the bulk sample to come to equilibrium (to help ensure moisture homogeneity). It should be noted that soil was mixed at the DELDOT facility in Bear with a concrete mixer. The soil was then placed in buckets and brought to the Soil Lab at the University of Delaware.

2) Weigh the dry empty mold and record its mass.

3) Place the soil in lifts in the mold (See Table 5.1 for the number of lifts that were used for each mold that was tested).

4) Compact the soil after each lift with a tamper by hand from a height of 16 to 18 inches.

5) Weigh the mold that is filled with the moist tamped soil and record its mass.

6) Setup the EDG and drive the EDG electrical probes and temperature probe into the soil in the mold (Figure 5.2).

7) Take electrical measurements with the EDG that can be used for the “soil model” calibration process (following the procedure outlined in Chapter 3).
Figure 5.4  Typical EDG setup in Mold

Twelve (12) mold calibration tests were conducted to build a soil model for the material being tested. In order to achieve a wide range of densities, various numbers of lifts and blows per lift were performed. Table 5.2 summarizes the number of lifts, blows per lift, and the calculated physical data that was used for correlation to the electrical measurements taken by the EDG to build a soil model.
<table>
<thead>
<tr>
<th></th>
<th>Mold #1</th>
<th>Mold #2</th>
<th>Mold #3</th>
<th>Mold #4</th>
<th>Mold #5</th>
<th>Mold #6</th>
<th>Mold #7</th>
<th>Mold #8</th>
<th>Mold #9</th>
<th>Mold #10</th>
<th>Mold #11</th>
<th>Mold #12</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lifts</td>
<td>10</td>
<td>5</td>
<td>2</td>
<td>5</td>
<td>3</td>
<td>2</td>
<td>5</td>
<td>3</td>
<td>2</td>
<td>10</td>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>Blows per Lift</td>
<td>100</td>
<td>100</td>
<td>50</td>
<td>100</td>
<td>50</td>
<td>25</td>
<td>100</td>
<td>50</td>
<td>25</td>
<td>100</td>
<td>100</td>
<td>25</td>
</tr>
<tr>
<td>$\gamma_m$ (kN/m$^3$)</td>
<td>20.1</td>
<td>19.6</td>
<td>18.7</td>
<td>21.0</td>
<td>19.7</td>
<td>18.9</td>
<td>21.0</td>
<td>20.4</td>
<td>19.4</td>
<td>20.6</td>
<td>19.2</td>
<td>18.3</td>
</tr>
<tr>
<td>$\gamma_d$ (kN/m$^3$)</td>
<td>18.4</td>
<td>18.0</td>
<td>17.1</td>
<td>18.9</td>
<td>17.7</td>
<td>16.9</td>
<td>18.5</td>
<td>17.9</td>
<td>17.0</td>
<td>18.8</td>
<td>17.5</td>
<td>16.7</td>
</tr>
<tr>
<td>$W_w$ (kN/m$^3$)</td>
<td>1.6</td>
<td>1.7</td>
<td>1.5</td>
<td>2.2</td>
<td>2.0</td>
<td>1.9</td>
<td>2.5</td>
<td>2.5</td>
<td>2.3</td>
<td>1.8</td>
<td>1.7</td>
<td>1.6</td>
</tr>
<tr>
<td>$w$ (%)</td>
<td>8.8</td>
<td>9.2</td>
<td>9.0</td>
<td>11.1</td>
<td>11.2</td>
<td>11.1</td>
<td>13.8</td>
<td>14.0</td>
<td>13.8</td>
<td>9.3</td>
<td>9.6</td>
<td>9.6</td>
</tr>
</tbody>
</table>
5.4 Mold Calibration Results

The mold tests described in this section were conducted to create a soil model to use in making a “blind” assessment of the EDG’s effectiveness. A truly blind assessment of the type that is recommended is provided in Chapter 6.

Calibration curves for the soil model developed from the mold tests are presented in the following section. It should be noted that calibration curves are presented without the EDG temperature correction algorithm (TC OFF) and with the EDG temperature correction algorithm (TC ON).

As stated earlier in Chapter 4, it is not best practice to assess the effectiveness of the EDG when the calibration data set is the same as the assessment data set, but for research and understanding this method is presented again. Direct comparison of the EDG-predicted values with the measured physical data from the mold tests is presented in this section. 1:1 plots that compare MOLD measured values versus EDG predicted values are presented, along with relative error histogram plots between the measured and predicted values. The in-situ measured soil properties assessed in this study were: moist unit weight ($\gamma_m$), weight of water per unit volume ($W_W$), dry unit weight ($\gamma_d$), and moisture content ($w$).

5.4.1 Mold Soil Model: Calibration Curves

The associated calibration curves for the mold calibration soil model are presented in Figure 5.5. The coefficient of determination ($R^2$) values are presented on each graph in Figure 5.5 as well. It should be noted that the soil model calibration curves in Figure 5.5a and Figure 5.5b for the Mold Soil Model (TC OFF & TC ON), show an increase in $R^2$ from 0.4931 to 0.5463 when the EDG temperature correction
algorithm is applied. Table 5.3 provides a summary of the $R^2$ values, slopes, and intercepts of the calibration curves for the Mold Soil Model (TC OFF & TC ON).

Table 5.3  General Summary Table of Calibration Curves – Mold Soil Model

<table>
<thead>
<tr>
<th>Mold Soil Model</th>
<th>Calibration Curve</th>
<th>$R^2$</th>
<th>Slope</th>
<th>Intercept</th>
</tr>
</thead>
<tbody>
<tr>
<td>TC OFF $\gamma$-MOLD vs. Z</td>
<td>0.4931</td>
<td>-0.0086</td>
<td>26.1610</td>
<td></td>
</tr>
<tr>
<td>TC ON $\gamma$-MOLD vs. Z</td>
<td>0.5463</td>
<td>-0.0099</td>
<td>27.9314</td>
<td></td>
</tr>
<tr>
<td>TC OFF $W_w$-MOLD vs. C/R</td>
<td>0.7144</td>
<td>30.6340</td>
<td>0.8229</td>
<td></td>
</tr>
<tr>
<td>TC ON $W_w$-MOLD vs. C/R</td>
<td>0.6362</td>
<td>35.0898</td>
<td>0.7603</td>
<td></td>
</tr>
</tbody>
</table>
Figure 5.5  Calibration Curves – Mold Soil Model (TC OFF & TC ON)
a) Calibration Curve 1: \( \gamma_{m-NDG} vs. Z \)
b) Calibration Curve 2: \( W_{w-NDG} vs. C/R \)
5.4.2 Mold Soil: 1:1 Plots

The Mold Soil Model calibration curves were used to predict the EDG values that are presented in this section. Figure 5.6a shows MOLD measured moist unit weights ($\gamma_{m,MOLD}$) versus EDG predicted moist unit weights ($\gamma_{m,EDG}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 5.6b shows MOLD measured dry unit weights ($\gamma_{d,MOLD}$) versus EDG predicted dry unit weights ($\gamma_{d,EDG}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 5.6c shows MOLD measured weight of water per unit volume ($W_{W,MOLD}$) versus EDG predicted weight of water per unit volume ($W_{W,EDG}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). Figure 5.6d shows MOLD measured moisture content ($w_{MOLD}$) versus EDG predicted moisture content ($w_{EDG}$) with and without the EDG temperature correction algorithm applied (TC ON & TC OFF). It should be noted that the solid line in Figure 5.6a, 5.6b, 5.6c, and 5.6d is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$ in Figure 5.6a, 5.6b, and 5.6c, and ±0.5 % lines in Figure 5.6d for reference.

For the Mold Soil, the RMSE, CV(RMSE), and NRMSE values for moist unit weight and dry unit weight are slightly greater with no EDG temperature correction algorithm applied. The RMSE, CV(RMSE), and NRMSE values for weight of water per unit volume and moisture content are slightly greater with the EDG temperature correction algorithm applied. Table 5.4 summarizes the statistical values for the Mold Soil.
Figure 5.6  1:1 Plots – Mold Soil (TC OFF & TC ON)
   a) 1:1 Plot – Moist Unit Weight
   b) 1:1 Plot – Dry Unit Weight
   c) 1:1 Plot – Wt. of Water per Unit Volume
   d) 1:1 Plot – Moisture Content
Table 5.4  Summary of Statistical Measures – Mold Soil

<table>
<thead>
<tr>
<th></th>
<th>(TC OFF)</th>
<th></th>
<th></th>
<th>(TC ON)</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(\gamma_m)</td>
<td>(W_w)</td>
<td>(\gamma_d)</td>
<td>(w)</td>
<td>(\gamma_m)</td>
<td>(W_w)</td>
</tr>
<tr>
<td>RMSE</td>
<td>0.614</td>
<td>0.196</td>
<td>0.618</td>
<td>1.277</td>
<td>0.582</td>
<td>0.208</td>
</tr>
<tr>
<td>CV(RMSE)</td>
<td>0.031</td>
<td>0.101</td>
<td>0.035</td>
<td>0.117</td>
<td>0.029</td>
<td>0.107</td>
</tr>
<tr>
<td>NRMSE</td>
<td>0.228</td>
<td>0.195</td>
<td>0.288</td>
<td>0.246</td>
<td>0.216</td>
<td>0.207</td>
</tr>
</tbody>
</table>

5.4.3 Relative Error

Relative error is calculated by taking the value considered to be the “actual” value, subtracting it from the “predicted” value, and dividing the resulting difference by the “actual” value (Freedman 1998). (Equation 5.1):

\[
\text{Relative error}(\%) = \frac{MOLD_{VALUE} - EDG_{VALUE}}{MOLD_{VALUE}} \times 100
\]  

(5.1)

The following section shows histograms of the relative error calculated for moist unit weight, weight of water per unit volume, dry unit weight, and moisture content for the Mold Soil. A cumulative distribution function (CDF) is displayed on each histogram as well.

5.4.4 Relative Error Results: Mold Soil

Figure 5.7a is a histogram plot of relative error between \(\gamma_m\)-MOLD and \(\gamma_m\)-EDG (TC ON & TC OFF). For the Mold Soil with TC OFF, relative error values for
\( \gamma_m \) range from -4.39% to 4.78%, and for the Mold Soil with TC ON relative error values for \( \gamma_m \) range from -3.49% to 7.00%.

Figure 5.7b is a histogram plot of relative error between \( \gamma_d^{\text{MOLD}} \) and \( \gamma_d^{\text{EDG}} \) (TC ON & TC OFF). For the Mold Soil (TC OFF), relative error values for \( \gamma_d \) range from -4.96% to 5.65%, and for the Mold Soil (TC ON) relative error values for \( \gamma_d \) range from -4.42% to 7.39%.

Figure 5.7c is a histogram plot of relative error between \( W_{W^{\text{MOLD}}} \) and \( W_{W^{\text{EDG}}} \) (TC ON & TC OFF). For the Mold Soil (TC OFF), relative error values for \( W_w \) range from -29.77% to 8.66%, and for the Mold Soil (TC ON) relative error values for \( W_w \) range from -26.94% to 13.96%.

Figure 5.7d is a histogram plot of relative error between \( w^{\text{MOLD}} \) and \( w^{\text{EDG}} \) (TC ON & TC OFF). For the Mold Soil (TC OFF), relative error values for \( w \) range from -28.93% to 13.37%, and for the Mold Soil (TC ON), relative percent error values for \( w \) range from -25.27% to 17.64%.

Table 5.5 provides a summary of the minimum, maximum, range, and mean of the relative error histograms for the Mold Soil (TC ON & TC OFF).
<table>
<thead>
<tr>
<th></th>
<th>Mold Soil</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(TC OFF)</td>
<td></td>
<td>(TC ON)</td>
</tr>
<tr>
<td></td>
<td>γ&lt;sub&gt;m&lt;/sub&gt;</td>
<td>W&lt;sub&gt;w&lt;/sub&gt;</td>
<td>γ&lt;sub&gt;d&lt;/sub&gt;</td>
</tr>
<tr>
<td>MIN</td>
<td>-4.39</td>
<td>-29.77</td>
<td>-4.96</td>
</tr>
<tr>
<td>MAX</td>
<td>4.78</td>
<td>8.66</td>
<td>5.65</td>
</tr>
<tr>
<td>RANGE</td>
<td>9.18</td>
<td>38.43</td>
<td>10.60</td>
</tr>
<tr>
<td>AVG</td>
<td>-0.15</td>
<td>-3.90</td>
<td>0.15</td>
</tr>
</tbody>
</table>
Figure 5.7  Relative Error Histograms and CDF Plots – Mold Soil
   a) Histogram & CDF – Moist Unit Weight (TC OFF & TC ON)
   b) Histogram & CDF – Dry Unit Weight (TC OFF & TC ON)
   c) Histogram & CDF – Wt. of Water per Unit Volume (TC OFF & TC ON)
   d) Histogram & CDF – Moisture Content (TC OFF & TC ON)
5.4.5 Summary of Mold Results

The soil model created using the mold calibration procedure has $R^2$ values for the calibration curves that range from .4931 to .7144. The $R^2$ values for the temperature compensated calibration curves for this soil model were higher in one case and lower in the other case (Table 5.3). The RMSE, CV(RMSE), and NRMSE values were greater when no EDG temperature correction algorithm was applied in some cases, and were less in other cases. Differences in relative percent error between the MOLD and EDG predicted values for the calibration curves with and without the EDG temperature correction algorithm applied are generally minimal. In addition, the standard deviation from the average for each set of EDG predicted values (TC ON & TC OFF) is lower than the standard deviation from the average for the corresponding MOLD measured values; this observation manifests itself as a smoothing effect, which can be observed on some of the 1:1 plots in this section. Table 5.6 provides a summary of the standard deviation values for the Mold Soil.

<table>
<thead>
<tr>
<th>Mold Soil: Standard Deviation, $\sigma_d$</th>
<th>$\gamma_m$</th>
<th>$W_w$</th>
<th>$\gamma_d$</th>
<th>$w$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MOLD</td>
<td>0.90</td>
<td>0.36</td>
<td>0.75</td>
<td>1.99</td>
</tr>
<tr>
<td>EDG (TC OFF)</td>
<td>0.63</td>
<td>0.33</td>
<td>0.32</td>
<td>1.65</td>
</tr>
<tr>
<td>EDG (TC ON)</td>
<td>0.67</td>
<td>0.29</td>
<td>0.43</td>
<td>1.45</td>
</tr>
</tbody>
</table>

5.5 Discussion of Results and Conclusions

From the raw data and associated analysis that is presented in this chapter, it is inherently evident that the raw physical data gathered from the mold tests has considerably less error associated with the test than its counterpart, the nuclear density
gauge test results using the field calibration method. Preparing molds for calibration tests in a controlled environment in a lab is a more reliable way to build a calibration data set and is considerably more trustworthy than physical data obtained from a nuclear density gauge or sand cone test. Generally, the agreement observed between the MOLD and EDG predicted values is relatively poor. This lack of agreement occurred even when the “assessment” data set was the same as the “calibration” data set, which is a much less rigorous test than a truly “blind” assessment (as discussed previously).

There are a number of possible causes for the general lack of agreement that was observed. Some of the more notable reasons that are believed to have been possible contributing factors in this mold calibration study include:

(1) The EDG electrical measurements of soil are believed to be very sensitive to the fines content of the soil. This is because the electrical characteristics of a soil matrix are significantly affected by the characteristics of the finer particles in the matrix. The fines content of the soil tested ranged from 11.44% to 18.22%, which is generally an acceptable variability in a given soil type, but may have a significant effect on the EDG electrical measurements.

(2) Once again, it is observed that the EDG temperature correction algorithm can lower the $R^2$ values for the calibration curves, thus not improving the results. The EDG temperature correction algorithm does not seem to properly capture the effect of temperature on the soil that was tested in this study.

A true “blind” assessment of the EDG using the soil model developed in this chapter will be discussed in detail in Chapter 6.
CHAPTER 6
SIMULATED FIELD TESTING PROCEDURE AND RESULTS

6.1 Introduction

As stated earlier in Chapter 4, it was very difficult to gather a wide range of field testing data on an active construction project. After this realization, a way to gather simulated field data was developed. To accomplish this task, a large, relatively stiff wooden box having inside dimensions of 1.52 m (5 ft) (Length), 0.91 m (3 ft) (Width), and 0.30 m (1 ft) (Height) was constructed. For each series of “field box” tests soil was placed in the rigid box and compacted with a walk-behind vibratory plate compactor prior to running in situ tests (Figure 6.1). A truly “blind” assessment of the EDG is performed and assessed in this chapter.
6.2 Soil Properties

The soil used for the large box testing was the same as the soil that was used for the mold calibration tests. This soil was from a borrow pit at the Greggo & Ferrara facilities in Delaware. A truckload of soil was donated by Greggo & Ferrarra and dumped at the DELDOT facility in Bear, Delaware for usage during this research study. Soil samples from the borrow pit were generally a brown silty sand with trace amounts of fine gravel (ASTM D 2488).

Sieve analysis tests were conducted in general accordance with ASTM D 6913 on samples from all 42 large box tests. From the results of these tests, thirty-four (34) soil samples were classified as silty sand (SM) and 8 soil samples were classified as poorly-graded sand with silt (SP-SM), according to the Unified Soil
Classification System (ASTM D 2487). Table 6.1 provides overall gradation information for the soil, as determined from the 42 samples that were analyzed from the mold tests. It should also be noted that the samples from the box are generally the same as the samples tested in the mold tests discussed in Chapter 5 (as shown in Figure 6.2).

![Gradation distributions for soil samples from large box and mold tests](image)

**Figure 6.2**  Gradation distributions for soil samples from large box and mold tests
Table 6.1  General Summary Table of Classification Results – Mold Tests

<table>
<thead>
<tr>
<th></th>
<th>MIN</th>
<th>MAX</th>
<th>MEAN</th>
<th>STD</th>
<th>CV (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. 4 (%)</td>
<td>89.63</td>
<td>97.95</td>
<td>96.10</td>
<td>1.57</td>
<td>1.63%</td>
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<tr>
<td>No. 10 (%)</td>
<td>86.93</td>
<td>94.85</td>
<td>92.87</td>
<td>1.50</td>
<td>1.62%</td>
</tr>
<tr>
<td>No. 40 (%)</td>
<td>45.04</td>
<td>53.72</td>
<td>50.24</td>
<td>2.22</td>
<td>4.43%</td>
</tr>
<tr>
<td>No. 200 (%)</td>
<td>13.88</td>
<td>18.74</td>
<td>15.62</td>
<td>0.96</td>
<td>6.16%</td>
</tr>
<tr>
<td>% gravel</td>
<td>2.05</td>
<td>10.37</td>
<td>3.90</td>
<td>1.57</td>
<td>40.16%</td>
</tr>
<tr>
<td>% sand</td>
<td>77.69</td>
<td>86.45</td>
<td>83.13</td>
<td>1.78</td>
<td>2.14%</td>
</tr>
<tr>
<td>% fines</td>
<td>11.13</td>
<td>16.09</td>
<td>12.97</td>
<td>1.02</td>
<td>7.88%</td>
</tr>
</tbody>
</table>

6.3 Large Box Testing Procedure

The large wooden box used to simulate field conditions was 1.52 m (5 ft) (Length) by 0.91 m (3 ft) (Width) by 0.30 m (1 ft) (Height). Standard 38 x 89 mm (2x4 in.) lumber and 13 mm (1/2 in.) plywood were used to construct the large box (Figure 6.1)

The following test procedure was followed when performing large box tests for this research study:

1) Prepare soil at desired moisture content and wait 30 minutes for equilibration.
   Soil was mixed at the DELDOT facility in Bear with a concrete mixer (Figure 6.3).

2) The soil was then placed in buckets for volume control and then dumped into the large wooden box (Figure 6.4).

3) In order to vary density in the large wooden box, it was found that varying lift thickness was the best way to achieve desired densities (unit weights). Either 3 or 6 passes were performed using a walk-behind vibratory plate compactor. Soil was placed in uniform lift thicknesses ranging from 25 mm (1 in.) to 102
mm (4 in.) and compacted with a walk behind vibratory plate compactor (See Table 6.2 for lift thicknesses, total lifts, and total number of passes per lift). Large cobbles and gravel were removed during fill placement to avoid any possible effects that these materials might have on the test results. (Figure 6.5).

4) Four (4) in-situ density tests were performed in a given test location. It should be noted that there were 3 test locations in each large box (Figure 6.6).

5) An electrical density gauge (EDG) test was performed in general accordance with ASTM D 7698 (Figure 6.7).

6) A nuclear density gauge (NDG) test using a Troxler 3440 Gauge was performed in general accordance with ASTM D 6938 (Figure 6.8).

7) A sand cone (SC) test was performed in general accordance with ASTM D 1556 (Figure 6.9).

8) A drive cylinder test (DC) was performed in general accordance with ASTM D 2937 (Figure 6.10 and 6.11).
Figure 6.3  Concrete Mixer used to mix soil to different moisture contents
Figure 6.4  Soil Placed in buckets for volume control

Figure 6.5  Soil Compacted with walk-behind vibratory plate compactor
Figure 6.6  Large box before performing in-situ density tests

Figure 6.7  EDG test performed in Large Box
Figure 6.8  NDG test performed in Large Box

Figure 6.9  Sand Cone test performed in Large Box
Figure 6.10  Drive Cylinder test performed in Large Box

Figure 6.11  Drive Cylinder after excavation from hole
Table 6.2 Physical Mold Calibration Data

<table>
<thead>
<tr>
<th>Box No.</th>
<th>Lift Thickness</th>
<th>Total Lifts</th>
<th>Passes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>51 mm (2 in.)</td>
<td>6</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>38 mm (1.5 in.)</td>
<td>9</td>
<td>6</td>
</tr>
<tr>
<td>3</td>
<td>51 mm (2 in.)</td>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>4</td>
<td>51 mm (2 in.)</td>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>5</td>
<td>76 mm (3 in.)</td>
<td>4</td>
<td>6</td>
</tr>
<tr>
<td>6</td>
<td>102 mm (4 in.)</td>
<td>3</td>
<td>3</td>
</tr>
<tr>
<td>7</td>
<td>51 mm (2 in.)</td>
<td>6</td>
<td>3</td>
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<td>8</td>
<td>25 mm (1 in.)</td>
<td>12</td>
<td>6</td>
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<td>9</td>
<td>76 mm (3 in.)</td>
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<td>10</td>
<td>76 mm (3 in.)</td>
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<td>11</td>
<td>25 mm (1 in.)</td>
<td>12</td>
<td>6</td>
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<tr>
<td>12</td>
<td>51 mm (2 in.)</td>
<td>6</td>
<td>3</td>
</tr>
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<td>51 mm (2 in.)</td>
<td>6</td>
<td>3</td>
</tr>
<tr>
<td>14</td>
<td>38 mm (1.5 in.)</td>
<td>9</td>
<td>6</td>
</tr>
</tbody>
</table>

6.4 Simulated Field Test Results: Large Box Tests

In order to establish a benchmark for comparing EDG test results with the results for the three more traditionally utilized field density tests, the results from the nuclear density gauge (NDG), sand cone (SC), and drive cylinder (DC) tests are presented first. For purposes of this study, the DC is assumed to be the “actual” value when comparing to the NDG or SC, and the NDG is assumed to be the “actual” value when comparing to the SC (these assumptions are based on the general scatter that was observed in the unit weight values for each of these tests).

6.4.1 Standard Large Box Tests

Figure 6.12 shows comparisons of measured moist unit weight for each of the traditional in situ density tests, as follows: NDG versus SC, NDG versus DC, and
SC versus DC. It should be noted that the solid line in Figure 6.12a, 6.12b, and 6.12c is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$.

Figure 6.13 shows comparisons of measured weight of water per unit volume for each of the traditional in situ density tests, as follows: NDG versus SC, DC versus NDG, and DC versus SC. It should be noted that the solid line in Figure 6.13a, 6.13b, and 6.13c is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$.

Figure 6.14 shows comparisons of measured dry unit weight for each of the traditional in situ density tests, as follows: NDG versus SC, DC versus NDG, and DC versus SC. It should be noted that the solid line in Figure 6.14a, 6.14b, and 6.14c is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$.

Figure 6.15 shows comparisons of measured moisture content for each of the traditional in situ density tests, as follows: NDG versus SC, DC versus NDG, and DC versus SC. It should be noted that the solid line in Figure 6.15a, 6.15b, and 6.15c is a 1:1 line, and the dashed lines are ±0.5 % lines.

The RMSE, CV(RMSE), and NRMSE values for moist unit weight, weight of water per unit volume, and dry unit weight are the lowest when comparing the DC versus NDG. The RMSE, CV(RMSE), and NRMSE values for moisture content are the lowest when comparing the DC versus SC. Table 6.3, Table 6.4, and Table 6.5 summarize the statistical values for the large box test comparisons that are presented in this section.
Figure 6.12 Standard Large Box Tests – Moist Unit Weight

a) NDG vs. SC: $\gamma_{m-\text{NDG}}$ vs. $\gamma_{m-\text{SC}}$

b) DC vs. NDG: $\gamma_{m-\text{DC}}$ vs. $\gamma_{m-\text{NDG}}$

c) DC vs. SC: $\gamma_{m-\text{DC}}$ vs. $\gamma_{m-\text{SC}}$
Figure 6.13  Standard Large Box Tests – Weight of Water per Unit Volume

a) NDG vs. SC: $W_{W,NDG}$ vs. $W_{W,SC}$
b) DC vs. NDG: $W_{W,DC}$ vs. $W_{W,NDG}$
c) DC vs. SC: $W_{W,DC}$ vs. $W_{W,SC}$
Figure 6.14  Standard Large Box Tests – Dry Unit Weight
   a) NDG vs. SC: $\gamma_{d\text{-NDG}}$ vs. $\gamma_{d\text{-SC}}$
   b) DC vs. NDG: $\gamma_{d\text{-DC}}$ vs. $\gamma_{d\text{-NDG}}$
   c) DC vs. SC: $\gamma_{d\text{-DC}}$ vs. $\gamma_{d\text{-SC}}$
Figure 6.15  Standard Large Box Tests – Moisture Content

a) NDG vs. SC: $w_{NDG}$ vs. $w_{SC}$
b) DC vs. NDG: $w_{DC}$ vs. $w_{NDG}$
c) DC vs. SC: $w_{DC}$ vs. $w_{SC}$
Table 6.3  Summary Table of Statistical Measures – NDG vs. SC

<table>
<thead>
<tr>
<th></th>
<th>$\gamma_m$</th>
<th>$W_w$</th>
<th>$\gamma_d$</th>
<th>$w$</th>
</tr>
</thead>
<tbody>
<tr>
<td>RMSE</td>
<td>1.373</td>
<td>0.203</td>
<td>1.203</td>
<td>0.686</td>
</tr>
<tr>
<td>CV(RMSE)</td>
<td>0.070</td>
<td>0.106</td>
<td>0.068</td>
<td>0.063</td>
</tr>
<tr>
<td>NRMSE</td>
<td>0.428</td>
<td>0.111</td>
<td>0.453</td>
<td>0.063</td>
</tr>
</tbody>
</table>

Table 6.4  Summary Table of Statistical Measures – DC vs. NDG

<table>
<thead>
<tr>
<th></th>
<th>$\gamma_m$</th>
<th>$W_w$</th>
<th>$\gamma_d$</th>
<th>$w$</th>
</tr>
</thead>
<tbody>
<tr>
<td>RMSE</td>
<td>0.497</td>
<td>0.138</td>
<td>0.458</td>
<td>0.810</td>
</tr>
<tr>
<td>CV(RMSE)</td>
<td>0.025</td>
<td>0.069</td>
<td>0.026</td>
<td>0.072</td>
</tr>
<tr>
<td>NRMSE</td>
<td>0.142</td>
<td>0.082</td>
<td>0.193</td>
<td>0.090</td>
</tr>
</tbody>
</table>

Table 6.5  Summary Table of Statistical Measures – DC vs. SC

<table>
<thead>
<tr>
<th></th>
<th>$\gamma_m$</th>
<th>$W_w$</th>
<th>$\gamma_d$</th>
<th>$w$</th>
</tr>
</thead>
<tbody>
<tr>
<td>RMSE</td>
<td>1.365</td>
<td>0.170</td>
<td>1.217</td>
<td>0.387</td>
</tr>
<tr>
<td>CV(RMSE)</td>
<td>0.069</td>
<td>0.086</td>
<td>0.069</td>
<td>0.035</td>
</tr>
<tr>
<td>NRMSE</td>
<td>0.390</td>
<td>0.101</td>
<td>0.514</td>
<td>0.043</td>
</tr>
</tbody>
</table>

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6.4.2 Standard Field Tests: Relative Error

Relative error is calculated by taking the value considered to be the “actual” value, subtracting it from the “predicted” value, and dividing the resulting difference by the “actual” value (Freedman 1998). The following three equations show how relative error was calculated in this section (Equation 6.1, 6.2, 6.3):

\[
\text{Relative error(\%)} = \frac{NDG_{\text{VALUE}} - SC_{\text{VALUE}}}{NDG_{\text{VALUE}}} \times 100
\]  

(6.1)

\[
\text{Relative error(\%)} = \frac{DC_{\text{VALUE}} - NDG_{\text{VALUE}}}{DC_{\text{VALUE}}} \times 100
\]  

(6.2)

\[
\text{Relative error(\%)} = \frac{DC_{\text{VALUE}} - SC_{\text{VALUE}}}{DC_{\text{VALUE}}} \times 100
\]  

(6.3)

The following section shows histograms of the relative error that is calculated for moist unit weight, weight of water per unit volume, dry unit weight, and moisture content for all of the standard field tests. A cumulative distribution function (CDF) is displayed on each histogram as well.

6.4.3 Standard Field Tests: Relative Error Results

Figure 6.16a is a histogram plot of relative error between $\gamma_m$-NDG and $\gamma_m$-SC, $\gamma_m$-DC and $\gamma_m$-NDG, and $\gamma_m$-DC and $\gamma_m$-SC. For NDG versus SC, relative error values for $\gamma_m$ range from -14.43\% to 3.72\%. For DC vs. NDG, relative error values for $\gamma_m$ range from -6.11\% to 3.21\%. For DC vs. SC, relative error values for $\gamma_m$ range from -9.08\% to 12.22\%.
Figure 6.16b is a histogram plot of relative error between $W_{W-NDG}$ and $W_{W-SC}$, $W_{W-DC}$ and $W_{W-NDG}$, and $W_{W-DC}$ and $W_{W-SC}$. For NDG vs. SC, relative error values for $W$ range from -24.26% to 8.19%. For DC vs. NDG, relative error values for $W$ range from -20.75% to 9.10%. For DC vs. SC, relative error values for $W$ range from -8.06% to 17.09%.

Figure 6.16c is a histogram plot of relative error between $\gamma_{d-NDG}$ and $\gamma_{d-SC}$, $\gamma_{d-DC}$ and $\gamma_{d-NDG}$, and $\gamma_{d-DC}$ and $\gamma_{d-SC}$. For NDG vs. SC, relative error values for $\gamma_d$ range from -14.10% to 4.36%. For DC vs. NDG, relative error values for $\gamma_d$ range from -5.54% to 3.96%. For DC vs. SC, relative error values for $\gamma_d$ range from -9.22% to 12.37%.

Figure 6.16d is a histogram plot of relative error between $w_{NDG}$ and $w_{SC}$, $w_{DC}$ and $w_{NDG}$, and $w_{DC}$ and $w_{SC}$. For NDG vs. SC, relative error values for $w$ range from -23.21% to 6.78%. For DC vs. NDG, relative error values for $w$ range from -20.73% to 9.87%. For DC vs. SC, relative error values for $w$ range from -8.89% to 7.07%.

Table 6.6, Table 6.7, and Table 6.8 provide a summary of the minimum, maximum, range, and mean of the relative error for all of the standard field tests.
Figure 6.16  Relative Error Histograms and CDF Plots – Standard Field Tests  
a) Histogram & CDF – Moist Unit Weight  
b) Histogram & CDF – Dry Unit Weight  
c) Histogram & CDF – Wt. of Water per Unit Volume  
d) Histogram & CDF - Moisture Content
### Table 6.6 Summary Table of Relative Error (%) – NDG vs. SC

<table>
<thead>
<tr>
<th></th>
<th>( \gamma_m )</th>
<th>( W_w )</th>
<th>( \gamma_d )</th>
<th>( w )</th>
</tr>
</thead>
<tbody>
<tr>
<td>MIN</td>
<td>-14.43</td>
<td>-24.26</td>
<td>-14.10</td>
<td>-23.21</td>
</tr>
<tr>
<td>MAX</td>
<td>3.72</td>
<td>8.19</td>
<td>4.36</td>
<td>6.78</td>
</tr>
<tr>
<td>RANGE</td>
<td>18.15</td>
<td>32.45</td>
<td>18.46</td>
<td>29.99</td>
</tr>
<tr>
<td>MEAN</td>
<td>-5.06</td>
<td>-9.62</td>
<td>-4.66</td>
<td>-4.73</td>
</tr>
</tbody>
</table>

### Table 6.7 Summary Table of Relative Error (%) – DC vs. NDG

<table>
<thead>
<tr>
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<th>( \gamma_m )</th>
<th>( W_w )</th>
<th>( \gamma_d )</th>
<th>( w )</th>
</tr>
</thead>
<tbody>
<tr>
<td>MIN</td>
<td>-6.11</td>
<td>-20.75</td>
<td>-5.54</td>
<td>-20.73</td>
</tr>
<tr>
<td>MAX</td>
<td>3.21</td>
<td>9.10</td>
<td>3.96</td>
<td>9.87</td>
</tr>
<tr>
<td>RANGE</td>
<td>9.33</td>
<td>29.85</td>
<td>9.50</td>
<td>30.60</td>
</tr>
<tr>
<td>MEAN</td>
<td>-0.56</td>
<td>-4.53</td>
<td>-0.25</td>
<td>-4.19</td>
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### Table 6.8 Summary Table of Relative Error (%) – DC vs. SC

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6.5 “Blind” Assessment of EDG

The following section uses the calibration relationships developed using the large mold tests (see Chapter 5) as a Soil Model for the EDG tests run in the large box tests. The following assessment is a truly “blind” assessment of how well the EDG performs, and is the recommended way to assess the EDG’s performance.

6.5.1 EDG Large Box Test Results

Figure 6.17 shows NDG versus EDG, SC versus EDG, and DC versus EDG measured moist unit weight with and without the EDG temperature correction applied (TC ON & TC OFF). It should be noted that the solid line in Figure 6.17a, 6.17b, and 6.17c is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$.

Figure 6.13 shows NDG versus EDG, SC versus EDG, and DC versus EDG measured weight of water per unit volume with and without the EDG temperature correction applied (TC ON & TC OFF). It should be noted that the solid line in Figure 6.13a, 6.13b, and 6.13c is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$.

Figure 6.14 shows NDG versus EDG, SC versus EDG, and DC versus EDG measured dry unit weight with and without the EDG temperature correction applied (TC ON & TC OFF). It should be noted that the solid line in Figure 6.14a, 6.14b, and 6.14c is a 1:1 line, and the dashed lines are ±0.5 kN/m$^3$.

Figure 6.15 shows NDG versus EDG, SC versus EDG, and DC versus EDG measured moisture content with and without the EDG temperature correction applied (TC ON & TC OFF). It should be noted that the solid line in Figure 6.15a, 6.15b, and 6.15c is a 1:1 line, and the dashed lines are ±0.5 %. The RMSE, CV(RMSE), and NRMSE values for moist unit weight, weight of water per unit.
volume, and moisture content generally become lower when the EDG temperature correction is applied when comparing the EDG to all 3 standard field tests. The RMSE, CV(RMSE), and NRMSE values for dry unit weight generally become higher when the EDG temperature correction is applied when comparing the EDG to all 3 standard field tests. Table 6.9, Table 6.10, and Table 6.11 summarize the statistical values for all of the large box test comparisons that are presented in this section.
Figure 6.17 Simulated Field Test Results – Moist Unit Weight

a) NDG vs. EDG: $\gamma_{m-NDG}$ vs. $\gamma_{m-EDG}$
b) SC vs. EDG: $\gamma_{m-SC}$ vs. $\gamma_{m-EDG}$
c) DC vs. EDG: $\gamma_{m-DC}$ vs. $\gamma_{m-EDG}$
Figure 6.18  Simulated Field Test Results – Weight of Water per Unit Volume

a) NDG vs. EDG: \( W_{W-NDG} \) vs. \( W_{W-EDG} \)

b) SC vs. EDG: \( W_{W-SC} \) vs. \( W_{W-EDG} \)

c) DC vs. EDG: \( W_{W-DC} \) vs. \( W_{W-EDG} \)
Figure 6.19  Simulated Field Test Results – Dry Unit Weight

a) NDG vs. EDG: $\gamma_d$-NDG vs. $\gamma_d$-EDG
b) SC vs. EDG: $\gamma_d$-SC vs. $\gamma_d$-EDG
c) DC vs. EDG: $\gamma_d$-DC vs. $\gamma_d$-EDG
Figure 6.20  Simulated Field Test Results – Moisture Content
a) NDG vs. EDG: $w_{\text{NDG}}$ vs. $w_{\text{EDG}}$

b) SC vs. EDG: $w_{\text{SC}}$ vs. $w_{\text{EDG}}$

c) DC vs. EDG: $w_{\text{DC}}$ vs. $w_{\text{EDG}}$
Table 6.9  Summary Table of Statistical Measures – NDG vs. EDG

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Table 6.10  Summary Table of Statistical Measures – SC vs. EDG

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Table 6.11  Summary Table of Statistical Measures – DC vs. EDG

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<td>0.417</td>
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6.5.2  EDG Large Box Tests: Relative Error

Relative error is calculated by taking the value considered to be the “actual” value, subtracting it from the “predicted” value, and dividing the resulting difference by the “actual” value (Freedman 1998). The following three equations show how relative error was calculated in this section (Equation 6.4, 6.5, 6.6):

\[
\text{Relative error} \%(\%) = \frac{\text{NDG}_{\text{VALUE}} - \text{EDG}_{\text{VALUE}}}{\text{NDG}_{\text{VALUE}}} \times 100 \quad (6.4)
\]

\[
\text{Relative error} \%(\%) = \frac{\text{SC}_{\text{VALUE}} - \text{EDG}_{\text{VALUE}}}{\text{SC}_{\text{VALUE}}} \times 100 \quad (6.5)
\]

\[
\text{Relative error} \%(\%) = \frac{\text{DC}_{\text{VALUE}} - \text{EDG}_{\text{VALUE}}}{\text{DC}_{\text{VALUE}}} \times 100 \quad (6.6)
\]

The following section shows histograms of the relative error calculated for moist unit weight, weight of water per unit volume, dry unit weight, and moisture content for all of the EDG large box tests. A cumulative distribution function (CDF) is displayed on each histogram as well.

6.5.3  EDG Large Box Tests: Relative Error Results

Figure 6.21a is a histogram plot of relative error between \( \gamma_{m-\text{NDG}} \) and \( \gamma_{m-\text{EDG}} \) (TC ON and TC OFF). For NDG vs. EDG (TC OFF), relative error values for \( \gamma_{m} \) range from -12.28\% to 3.38\% and for NDG vs. EDG (TC ON), relative error values for \( \gamma_{m} \) range from -10.55\% to 13.78\%.

Figure 6.21b is a histogram plot of relative error between \( W_{W-\text{NDG}} \) and \( W_{W-\text{EDG}} \) (TC ON and TC OFF). For NDG VS. EDG (TC OFF), relative error values
for $W_w$ range from -77.47% to -11.71% and for NDG VS. EDG (TC ON), relative error values for $W_w$ range from -56.42% to -6.64%.

Figure 6.21c is a histogram plot of relative error between $\gamma_d$-NDG and $\gamma_d$-EDG (TC ON and TC OFF). For NDG vs. EDG (TC OFF), relative error values for $\gamma_d$ range from -11.08% to 5.64% and for NDG vs. EDG (TC ON), relative error values for $\gamma_d$ range from -10.83% to 15.66%.

Figure 6.21d is a histogram plot of relative error between $w_{\text{NDG}}$ and $w_{\text{EDG}}$ (TC ON and TC OFF). For NDG vs. EDG (TC OFF), relative error values for $w$ range from -67.20% to -3.41% and for NDG vs. EDG (TC ON), relative error values for $w$ range from -56.30% to 2.15%.

Figure 6.22a is a histogram plot of relative error between $\gamma_m$-SC and $\gamma_m$-EDG (TC ON and TC OFF). For SC vs. EDG (TC OFF), relative error values for $\gamma_m$ range from -12.33% to 12.49% and for SC vs. EDG (TC ON), relative error values for $\gamma_m$ range from -9.43% to 20.94%.

Figure 6.22b is a histogram plot of relative error between $W_w$-SC and $W_w$-EDG (TC ON and TC OFF). For SC vs. EDG (TC OFF), relative error values for $W_w$ range from -56.40% to 3.98% and for SC vs. EDG (TC ON), relative error values for $W_w$ range from -46.72% to 9.59%.

Figure 6.22c is a histogram plot of relative error between $\gamma_d$-SC and $\gamma_d$-EDG (TC ON and TC OFF). For SC vs. EDG (TC OFF), relative error values for $\gamma_d$ range from -6.67% to 14.97% and for SC vs. EDG (TC ON), relative error values for $\gamma_d$ range from -5.60% to 21.75%.

Figure 6.22d is a histogram plot of relative error between $w_{\text{SC}}$ and $w_{\text{EDG}}$ (TC ON and TC OFF). For SC vs. EDG (TC OFF), relative error values for $w$ range
from -57.91% to 4.26% and for SC vs. EDG (TC ON), relative error values for $w$ range from -49.86% to 8.89%.

Figure 6.23a is a histogram plot of relative error between $\gamma_{m-DC}$ and $\gamma_{m-EDG}$ (TC ON and TC OFF). For DC vs. EDG (TC OFF), relative error values for $\gamma_m$ range from -11.33% to 7.87% and for DC vs. EDG (TC ON), relative error values for $\gamma_m$ range from -8.01% to 17.03%.

Figure 6.23b is a histogram plot of relative error between $W_{W-DC}$ and $W_{W-EDG}$ (TC ON and TC OFF). For DC vs. EDG (TC OFF), relative error values for $W_W$ range from -63.50% to -1.78% and for DC vs. EDG (TC ON), relative error values for $W_W$ range from -48.59% to 3.30%.

Figure 6.23c is a histogram plot of relative error between $\gamma_{d-DC}$ and $\gamma_{d-EDG}$ (TC ON and TC OFF). For DC vs. EDG (TC OFF), relative error values for $\gamma_d$ range from -8.76% to 9.00% and for DC vs. EDG (TC ON), relative error values for $\gamma_d$ range from -8.58% to 18.04%.

Figure 6.23d is a histogram plot of relative error between $w_{DC}$ and $w_{EDG}$ (TC ON and TC OFF). For DC vs. EDG (TC OFF), relative error values for $w$ range from -56.95% to 6.57% and for DC vs. EDG (TC ON), relative error values for $w$ range from -49.87% to 11.19%.

Table 6.12, Table 6.13, and Table 6.14 provide a summary of the minimum, maximum, range, and mean of the relative error for all of the EDG large box tests.
Figure 6.21 Relative Error Histograms and CDF Plots – NDG vs. EDG
a) Histogram & CDF – Moist Unit Weight
b) Histogram & CDF – Dry Unit Weight
c) Histogram & CDF – Wt. of Water per Unit Volume
d) Histogram & CDF - Moisture Content
Figure 6.22  Relative Error Histograms and CDF Plots – SC vs. EDG
   a) Histogram & CDF – Moist Unit Weight
   b) Histogram & CDF – Dry Unit Weight
   c) Histogram & CDF – Wt. of Water per Unit Volume
   d) Histogram & CDF - Moisture Content
Figure 6.23  Relative Error Histograms and CDF Plots – DC vs. EDG
a) Histogram & CDF – Moist Unit Weight
b) Histogram & CDF – Dry Unit Weight
c) Histogram & CDF – Wt. of Water per Unit Volume
d) Histogram & CDF - Moisture Content
Table 6.12  Summary Table of Relative Error (%) – NDG vs. EDG

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Table 6.13  Summary Table of Relative Error (%) – SC vs. EDG

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Table 6.14  Summary Table of Relative Error (%) – DC vs. EDG

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6.6 Summary of Large Box Test Results

The nuclear density gauge and drive cylinder tests generally have the best agreement out of all of the tests for moist unit weight, weight of water per unit volume, and dry unit weight. The moisture content determined from the sand cone test and the drive cylinder test had the best agreement. Generally, the “blind” assessment tests that were conducted using the EDG showed relatively poor agreement between the EDG-predicted values and the NDG, SC, or DC tests (worse than the results obtained from some of the more traditional density-based tests such as the NDG or DC), for EDG tests that were conducted using the soil model determined from the mold calibration process. It should be noted that the minimum, maximum, and mean relative error (%) for weight of water per unit volume and moisture content are extremely high, which indicates that the calibration curve that was established to determine the weight of water per unit volume and moisture content for the EDG tests did not do a good job of capturing the in situ soil properties in the large box.

6.7 Large Box Test Data Subset

It should be noted that 12 of the 42 large box tests that were performed fell outside of the data set that was used for mold calibration. In general, it is not best practice to use calibration curves to predict test points outside of the range of data that is used for calibration. Consequently, the same analyses that are described in the previous sections were performed excluding the points that fell outside of the calibration range; the results yielded no significant differences in the EDG’s performance than what is generally described in the previous sections. For general comparison purposes, summary tables of statistical measures and relative error (%) values are provided in Tables 6.15 through Table 6.20.
Table 6.15  Summary Table of Statistical Measures (All Data Within Calibration Range) – NDG vs. EDG

NDG vs. EDG

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<td>(w)</td>
</tr>
<tr>
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<td>0.757</td>
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<td>NRMSE</td>
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Table 6.16  Summary Table of Statistical Measures (All Data Within Calibration Range) – SC vs. EDG

SC vs. EDG

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<td>NRMSE</td>
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Table 6.17  Summary Table of Statistical Measures (All Data Within Calibration Range) – DC vs. EDG

DC vs. EDG

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<td>0.407</td>
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121
### Table 6.18  Summary Table of Relative Error (%) (All Data Within Calibration Range) – NDG vs. EDG

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</table>

### Table 6.19  Summary Table of Relative Error (%) (All Data Within Calibration Range) – SC vs. EDG

<table>
<thead>
<tr>
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<th>(TC OFF)</th>
<th>(TC ON)</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>$\gamma_m$</td>
<td>$W_w$</td>
</tr>
<tr>
<td>MIN</td>
<td>-12.33</td>
<td>-56.40</td>
</tr>
<tr>
<td>MAX</td>
<td>10.78</td>
<td>3.98</td>
</tr>
<tr>
<td>RANGE</td>
<td>23.11</td>
<td>60.38</td>
</tr>
<tr>
<td>MEAN</td>
<td>0.57</td>
<td>-22.90</td>
</tr>
</tbody>
</table>

### Table 6.20  Summary Table of Relative Error (%) (All Data Within Calibration Range) – DC vs. EDG

<table>
<thead>
<tr>
<th></th>
<th>(TC OFF)</th>
<th>(TC ON)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\gamma_m$</td>
<td>$W_w$</td>
</tr>
<tr>
<td>MIN</td>
<td>-10.64</td>
<td>-63.50</td>
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<tr>
<td>MAX</td>
<td>0.85</td>
<td>-1.78</td>
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<tr>
<td>RANGE</td>
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<td>61.72</td>
</tr>
<tr>
<td>MEAN</td>
<td>-4.30</td>
<td>-29.21</td>
</tr>
</tbody>
</table>
6.8 Discussion of Results and Conclusions

From the raw data and associated analysis that are presented in this chapter, it is inherently evident that the electrical density gauge (EDG) provides results with higher RMSE, CV(RMSE), NRMSE, and relative error (%) values than its comparable in situ density-based testing counterparts, particularly the nuclear density gauge (NDG) and drive cylinder (DC) tests. Further, the temperature compensation algorithm tends not to produce a significantly marked improvement in the EDG test results. However on the plus side, from the results that are provided, the EDG may yield better predictions of moist unit weight and dry unit weight than those that can be obtained from the sand cone (SC) test. It should be noted that these conclusions were made for a true blind assessment of the EDG, with the mold calibration procedure, default on-board calibration relationships, and the default temperature compensation algorithm. It may be possible to significantly improve the results from EDG tests if alternative calibration procedures, calibration relationships, or temperature correction algorithms are used. For future studies, we will focus our efforts in this area, in order to yield enhanced EDG characterization capabilities.
Chapter 7

CONCLUSIONS AND RECOMMENDATIONS

7.1 Conclusions

The effectiveness and accuracy of the Electrical Density Gauge (EDG) was evaluated in this research project. A preliminary field study was performed on two active construction projects in Dover, DE and Middletown, DE. Evaluation of the in-situ testing process and data gathered during this preliminary study led to the following conclusions:

- It is difficult to construct a soil model using a field calibration process that spans the potential range of moisture contents and soil densities that could be encountered during the field compaction process. This is in part because of the fact that, on a typical roadway project, contractors try to maintain the same moisture content and reach the same density for the fill material they are compacting. This creates a difficulty when trying to build a soil model that spans the range of densities and moisture contents that may be encountered in a fair and representative way. Getting the field variability in moisture content that is necessary to build a good moisture calibration relationship for the EDG can be particularly challenging under certain field conditions.

- There are inherent uncertainties and sources of error in the tests that are used for field calibration of the EDG. In particular, the field calibration
process requires the use of a NDG or other standard in-situ density test like the sand cone or rubber balloon test. These tests have their own uncertainty and sources of error in measurement, and consequently this error has the potential to become compounded when building a soil model. This means that the accuracy of the EDG can never be more than the accuracy of the test which it is calibrated against, which has the potential to limit the EDG’s capabilities (e.g., it may be possible to achieve more accurate results with the EDG than those from the SC or NDG test, but this cannot be achieved if other tests are being used for EDG calibration). Further, the necessity of having to use the NDG as part of the EDG calibration process necessitates that DelDOT remain compliant with Nuclear Regulatory Commission (NRC) guidelines, which partially defeats some of the potential advantages of the EDG.

- Soil variability on a given construction project can cause difficulties when trying to build a soil model with the EDG. In particular, the EDG appears to be more sensitive than the NDG to variations in the soil borrow source. This effect is evident if the results from the Dover project are compared against those from the Middletown project. Changes in the quantity or nature of the fines in a borrow soil are believed to have a significant effect on measured EDG results. This is because the electrical characteristics of a soil matrix are significantly affected by the characteristics of the finer particles in the matrix.

- From preliminary data, it is evident that the EDG temperature correction algorithm can lower the $R^2$ values for the calibration curves,
thus not improving the results. The EDG temperature correction algorithm does not seem to properly capture the effect of temperature on the soils that were tested in the preliminary field study.

After considerable time was spent trying to acquire the necessary data on these two active construction projects to fairly assess the EDG, it was determined that this approach was not the most desirable. The inability to control moisture content and temperature of the soil precisely in the field, as well as practical contractual requirements which necessitated that EDG calibration should not significantly slow the process of field construction led to development of a second experimental study for calibration and assessment of the EDG. Large box testing of soil in conjunction with large mold testing was performed to acquire the necessary data to evaluate the accuracy of the EDG. The evaluation of the mold calibration procedure and “large” box testing indicated the following:

- EDG electrical measurements of soil are believed to be very sensitive to the fines content of the soil. The electrical characteristics of a soil matrix are significantly affected by the nature of the finer particles in the matrix, and may have a significant effect on the EDG electrical measurements.
- From the density based tests that were conducted (EDG, NDG, sand cone (SC), and drive cylinder (DC)), the nuclear density gauge and drive cylinder tests generally have the best agreement out of all of the tests for moist unit weight, weight of water per unit volume, and dry unit weight.
- The moisture content determined from the sand cone test and the drive cylinder test had the best agreement.
- When compared with the drive cylinder (DC) test, the electrical density gauge (EDG) provides results with higher RMSE, CV(RMSE), NRMSE, and relative error (%) values than its comparable in situ density-based testing counterparts, particularly the nuclear density gauge (NDG).
- The EDG temperature correction algorithm tends not to produce a significantly marked improvement in the EDG test results. The default EDG temperature correction algorithm does not seem to properly capture the effect of temperature on the soils that were tested in this study.

7.2 Recommendations

For future utilization of the Electrical Density Gauge by the Delaware DOT, the following recommendation is made:
- To further evaluate the accuracy and effectiveness of the EDG, extra field studies are needed on a variety of commonly used soils and other construction materials utilized by the DOT for road-embankment construction to confirm the results that were observed in this initial evaluation study.
7.3 Future Research

It may be possible to improve the results obtained from EDG tests if alternative calibration relationships, calibration procedures, or temperature correction algorithms are used. For future studies, we will focus our efforts in this area, in order to yield enhanced EDG characterization capabilities.
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