

## PHY 342 HW Ch.4b

Do problem 4.10\*, 4.11, 4.15 plus the following (\*=optional bonus).

q4.5

For the particle in the 3D infinite spherical well, the wave function for  $l = 0$  ( $s$ -state) is

$$\psi_{n00} = A \frac{\sin(n\pi r/a)}{r} Y_{00}.$$

Determine the normalization constant  $A$ .

q4.6

For  $l \neq 0$  states in the 3D infinite spherical well, the eigenenergies are determined by the zeros of  $j_l(ka)$ , or  $k_{nl} = x_{nl}/a$  with  $x_{nl}$  being the  $n$ -th zero of the spherical Bessel function  $j_l(x)$ .

Search for “Scipy zeros spherical Bessel function”, or follow this link

[https://docs.scipy.org/doc/scipy/reference/generated/scipy.special.spherical\\_jn.html](https://docs.scipy.org/doc/scipy/reference/generated/scipy.special.spherical_jn.html)

to write a program to obtain graphically (or numerically with root finding) the first 5 zeros of  $j_l(x)$  for  $l = 1, 2, 3$ . Then give the energies  $E_{nl}$  for each  $l$  in units of  $\hbar^2\pi^2/2ma^2$ . Sketch the energy levels, with  $n$  being the vertical axis and  $l$  the horizontal axis including  $l = 0$ .

q4.7

(a) Plot the radial wave functions  $R_{20}$  and  $R_{21}$  using a computer. Omit the  $a^{-3/2}$  factor, and use Bohr radius as the units for  $r$ .

(b) Plot the radial probability distributions, i.e.,  $|R_{nl}|^2 r^2$ , for the two cases. Restrict  $0 \leq r/a \leq 10$ .

q4.8

Derive the most probable value of  $r$  for finding the electron in the states  $R_{20}$  and  $R_{21}$ . Note this is different than the highest probability density. Compare and discuss your answers with the graphs above.