Increasing informativeness and reducing ambiguities: Adaptive strategies in human information processing

Vladimir M. Sloutsky (sloutsky.1@osu.edu)
College of Education and Center for Cognitive Science; 1945 N. High Street
Columbus, OH 43210, USA

Aaron W. Rader (rader.34@osu.edu)
Department of Psychology and Center for Cognitive Science; 1885 Neil Ave.
Columbus, OH 43210, USA

Bradley J. Morris (Morris.243@osu.edu)
Department of Human Development and Center for Cognitive Science; 1787 Neil Ave.
Columbus, OH 43210, USA

Abstract
How do people deal with ambiguity and indeterminacy of incoming information? The results of the two reported experiments indicate that both young children and adults tend to reduce ambiguity, systematically ‘converting’ non-informative propositions into more informative ones. Although young children and older participants use different strategies, high rates of conversions were found in both groups. These conversions seem to represent an adaptive cognitive constraint — a tendency to reduce ambiguity and to increase the informativeness of incoming information.

Introduction
It is well known that people commit multiple errors when reasoning and making judgments (Evans & Over, 1996; for review). For example, when processing deductive arguments, they tend to deviate from the argument’s logic, confusing familiar or believable conclusions with logically necessary ones; they also commit various logical fallacies in reasoning with conditionals (Evans, Newstead, & Byrne, 1993). Traditionally these errors have been explained as resulting from a variety of random factors (e.g., fluctuations of attention) and from reasoners’ tendency to misconstrue some premises in accordance with conversational uses of connectives (e.g., reasoners may mistake a premise “If P then Q” for “If and only if P then Q”) (Braine & O’Brien, 1991; Rips 1994). However, these deviations exhibit amazing regularity and systematicity for purely random fluctuations. In this paper we argue that some of these errors may stem from an adaptive strategy people use when dealing with uncertainty and ambiguity. This strategy may result in certain distortions of incoming information, but it allows reductions in the uncertainty and ambiguity of the environment.

This tendency to reduce ambiguity seems to be a general property of cognitive systems whose function is to process information from the environment, and to adequately navigate the organism using available environmental cues. There is ample evidence that both human and animal species tend to avoid nondiagnostic cues, those that do not allow the organism to discriminate among different objects or classes, and highly variable cues, those that may or may not be present in the same object or class (see Estes, 1988; 1994, for reviews). For example, the red color of the tomato does not allow one to distinguish the tomato from other red vegetables (nondiagnosticity), whereas the changing color of the chameleon does not help in identifying this animal (high variability). This tendency is especially apparent in human cognition that relies heavily on linguistic representations. A number of authors (Gibson, 1940, Shepard, Holovad & Jenkings, 1961) have demonstrated that the difficulty of learning a classification increases if the stimuli that are assigned to different classes are less discriminable (nondiagnosticity), or if stimuli that are assigned to the same class are more discriminable (highly variable). Similar difficulties have been demonstrated in concept attainment (Bruner, Goodnow, & Austin, 1956; Estes, 1994), reasoning and problem solving (Fay & Klahr 1996, Evans & Over, 1996), and early word learning (Markman, 1990). We hypothesize that these difficulties may represent an adaptive cognitive constraint. This constraint prohibits the organism from acquiring ambiguous, indeterminate information, which cannot be readily used to adapt to the environment, thus directing learning toward acquisition of more useful and less ambiguous information. In other words, the organism’s spontaneous learning might be limited to those cues that better inform the organism about the environment. At the same time, human discourse is replete with ambiguities and indeterminacies — people use various propositional forms that do not unambiguously inform about states of the world. For example, the proposition “Either theory A or theory B is true” is ambiguous with respect to theory selection. Ambiguous propositions (e.g., “it is either blue or green”) are less informative with respect to the environment than more determinate ones (e.g., “it is green”).

The formal treatment of informativeness was proposed in semantics. Bar-Hillel and Carnap (1964) defined informativeness of a proposition to be a function of the number of states of the world that the proposition rules out.
Table 1: Informativeness of propositions varying in their logical form.

<table>
<thead>
<tr>
<th>Proposition</th>
<th>Form</th>
<th>Example</th>
<th>Proportion of states of the world ruled out by the proposition</th>
<th>N of states of the world where the proposition is true (ΣTj)</th>
<th>Logical Probability (ΣTj/2^n)</th>
<th>Informativeness (- log2 P(i))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Affirmation</td>
<td>A</td>
<td>I drank tea this morning</td>
<td>.5</td>
<td>1</td>
<td>.5</td>
<td>1</td>
</tr>
<tr>
<td>Negation</td>
<td>Not-A</td>
<td>I did not drink tea this morning</td>
<td>.5</td>
<td>1</td>
<td>.5</td>
<td>1</td>
</tr>
<tr>
<td>Conjunction</td>
<td>A AND B</td>
<td>I drank tea AND coffee this morning</td>
<td>.75</td>
<td>1</td>
<td>.25</td>
<td>2</td>
</tr>
<tr>
<td>Disjunction (inclusive)</td>
<td>A OR B</td>
<td>I drank tea OR coffee this morning</td>
<td>.25</td>
<td>3</td>
<td>.75</td>
<td>0.42</td>
</tr>
<tr>
<td>Disjunction (exclusive)</td>
<td>A OR B (but not both)</td>
<td>I drank EITHER tea OR coffee this morning</td>
<td>.5</td>
<td>2</td>
<td>.5</td>
<td>1</td>
</tr>
<tr>
<td>Conditional</td>
<td>IF A THEN B</td>
<td>IF I drank tea THEN I drank coffee</td>
<td>.25</td>
<td>3</td>
<td>.75</td>
<td>0.42</td>
</tr>
<tr>
<td>Bi-Conditional</td>
<td>IFF A THEN B</td>
<td>I drank coffee IF AND ONLY IF I drank tea</td>
<td>.5</td>
<td>2</td>
<td>.5</td>
<td>1</td>
</tr>
<tr>
<td>Tautology</td>
<td>A OR not-A</td>
<td>I drank tea this morning OR I did not drink tea this morning</td>
<td>0</td>
<td>4</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>Contradiction</td>
<td>A AND not-A</td>
<td>I drank tea this morning AND I did not drink tea this morning</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>Undefined</td>
</tr>
</tbody>
</table>

More precisely, the informativeness of a statement is inversely related to the logical probability of the statement (see, Bar-Hillel & Carnap, 1964; Johnson-Laird 1993), for discussions). According to Bar-Hillel (1964), the relations are specified by the following equation.

\[ \text{inf}(i) = - \log_2 P(i) \quad \text{Equation 1} \]

The logical probability of a statement is the number of states of the world where the proposition is true divided by the total number of all possible states of the world covered by the proposition. Thus, logical probability could be calculated using equation 2.

\[ P(i) = \frac{\Sigma T_j}{2^n} \quad \text{Equation 2} \]

\( T_j \) is a state of the world where the proposition is true and \( n \) is the number of atomic statements in the proposition. The informativeness of the most common forms of propositions is provided in Table 1. According to the table, a conjunction of two statements is more informative than an atomic assertion, a biconditional, and an exclusive disjunction, and these are more informative than a disjunction and a conditional. At the same time, a tautology is a totally non-informative statement, and informativeness of a contradiction is not defined.

It seems plausible that if the tendency to reduce ambiguity stems from a cognitive constraint, then people would try to reduce ambiguity of non-informative propositions by increasing their informativeness, and this tendency will be present early in their lives. In particular, they may change the propositional form of less informative propositions to increase informativeness. This tendency could be defined as conversion of less informative propositions into more informative ones. Therefore, we predicted that contradictions and tautologies would be converted more frequently than disjunctions, which, in turn would be converted more frequently than conjunctions. To test this hypothesis we designed tasks where young children and adults had to determine the truth status of more and less informative predictions (Experiment 1), and where adolescents and adults had to memorize and recall more and less informative propositions (Experiment 2). The goal of the two reported experiments was to test the hypothesis and to provide descriptive accounts of human conversion strategies.

**Experiment 1**

**Method**

**Participants** Two groups of participants were included in the design. The first group consisted of 34 four- and five-year old children currently enrolled in two child care centers in a large Midwestern city. These participants were selected on the basis of returning a parental consent form. The second group of participants included 31 undergraduate students currently enrolled in a large Midwestern university. These participants were recruited from introductory courses in a department of human development and family science.
Materials The experimental tasks consisted of a series of predictions by an imaginary character, ZZ (references to ZZ were omitted for the university students), as to the outcome of a ball dropped in the Tautology Machine. The Tautology Machine is a 36" x 24" board with a chute at the top in which a ball dropped will fall through several nails which direct the ball to one of two terminating points (the two chutes were marked with red and green colors). ZZ made predictions regarding the outcomes of the game. These predictions had syntactic forms of logical constants (tautologies and contradictions), and contingent statements (affirmations and negations). The following predictions were presented to subjects in four random orders:

- Tautology 1: The ball will NOT land on Red OR will land on Red.
- Tautology 2: The ball will land on Red OR will NOT land on Red.
- Contradiction 1: The ball will NOT land on Red AND will land on Red.
- Contradiction 2: The ball will land on Red AND will NOT land on Red.
- Negation: The ball will NOT land on Red.
- Affirmation: The ball will land on Red.

Procedure One within-subject variable, the form of the prediction, and age and gender as across-subject factors were included in the design. The experiment was conducted in a single 10-15 minute session that included two phases: warm-up/instruction phase and the experimental phase. Each participant was tested individually in a quiet room. Children were videotaped in order to ensure accurate coding of responses. In the warm-up phase, the participants were familiarized with the device. To ensure that the participants could distinguish between statements that were true and not true, they were also asked to evaluate two statements (one explicitly true and another explicitly false). In the experimental phase, the instructions and predictions were read to each participant and repeated if requested. The participants were asked three questions. First, they were asked to evaluate the a priori truth status of the prediction as “Not True”, “True”, or “Can’t Tell” (a priori evaluation). Then participants were asked if it was necessary to drop the ball to check the truth status of the a priori prediction, constituting the request for empirical verification (request for verification). If empirical verification was requested, then the ball was actually dropped through the machine. Finally, after the ball was dropped, the participants were asked to again evaluate the initial predictions as “Right”, “Wrong” or “Can’t Tell” (a posteriori evaluation).

Results and Discussion
Table 2 contains data on how the participants handled propositions of different logical form. These data indicate that children did not distinguish between logically true, logically false, and contingent statements. At the same time, university students consistently distinguished between